# Development of Fast Sampling Transient Recorders with Custom ASICs 

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# Development of Fast Sampling Transient Recorders with Custom ASICs 

A Dissertation<br>Submitted to the Faculty of Mathematics and Computer Science of the University of Mannheim<br>for the Degree of Doktor der Naturwissenschaften (Dr. rer. nat.)

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## Zusammenfassung

Analoge Speicher aus geschalteten Kapazitäten sind für eine Vielzahl von Anwendungen geeignet, sofern keine fortlaufende Digitalisierung der analogen Signale notwendig ist. In Datennahmesystemen, die auf einem analogen Speicher basieren, werden die Eingangssignale mit hoher Rate abgetastet und für begrenzte Zeit zwischengespeichert. Die analogen Abtastwerte werden dann mit einer geringeren Rate ausgelesen und mit einem langsamen ADC digitalisiert, bevor neue Signale aufgenommen werden. Die Vorteile eines analogen Speichers sind ein geringerer Leistungsverbrauch, geringere Kosten, eine große Dichte und ein höherer dynamischer Bereich bei hohen Abtastraten. Ein analoger Speicher führt die Abtastung und Zwischenspeicherung von Werten mit höheren Raten und grösserer Genauigkeit durch, als dies durch eine direkte digitale Umwandlung bewerkstelligt werden könnte.

Diese Dissertation untersucht detailliert die wichtigen Komponenten zweier analoger Speicher. Die Forschungsarbeit hat zum Entwurf von zwei analogen Speichern geführt, die Analogsignale mit einer Abtastrate von einigen hundert MHz aufnehmen können. Dies wird durch eine Speicherarchitektur bewerkstelligt, in der die Sockelwerte der Speicherzellen und die Abtastzeiten unabhängig vom Signalpegel sind. Die Ansteuerung der Schreibadresse für diese Speicher wurde durch Inverter-Verzögerungsketten realisiert, die eine hohe Güte bezüglich der Abtastrate und der Zeitgenauigkeit gewährleisten.

Auf Grundlage der in dieser Arbeit entwickelten Konzepte wurden zwei analoge Speicher entworfen und in der AMS $0.8 \mu \mathrm{~m}$ CMOS Technologie mit Poly-zu-Poly Kapazitäten integriert. Ausgedehnte Messungen dieser Prototypen bei einer Abtastrate von 500 MHz werden dargestellt. Nachdem ein einfaches Multiplikations - und Additionskorrekturverfahren durchgeführt wurde, entspricht der dynamische Bereich, die Linearität, der Offset und die Verstärkung einer Genauigkeit von 8 Bit.

## Abstract

Switched capacitor analog memories are well suited to a number of applications where a continuous digitisation of analog signals is not needed. In data acquisition systems based on the use of an analog memory, the input waveforms are sampled and stored at a high rate for a limited period of time, and the analog samples are then retrieved at a lower rate and digitised with a slow ADC before new waveforms are acquired. The advantages of using an analog memory are lower overall power dissipation and cost, high density, and potentially superior dynamic range at high sampling rates. The analog memory shows the fact that the sampling and storage of samples in analog memory cells can be accomplished at a higher rate and with a greater precision than direct digital conversion.

This dissertation examines the important components of two analog memories in detail. The research has led to the design of two analog memories that can acquire analog waveforms at sampling rates of several hundred MHz . This is accomplished by a memory architecture in which the memory cell pedestals and sampling times are independent of the signal level. The write address control for these memories has been realised with inverter delay chains that provide high performance with respect to sampling rate and timing accuracy.

Based upon the concepts developed in this work, two analog memories were designed and integrated in a AMS $0.8 \mu \mathrm{~m}$ CMOS technology with poly-to-poly capacitors. Extensive measurements of these prototypes at a sampling rate of 500 MHz are presented and demonstrate a dynamic range, linearity, offset, and gain accuracy corresponding to a precision of 8 bits after a simple multiplication and addition correction procedure.

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## Chapter 1

## Introduction

### 1.1 Motivation

In many modern data acquisition systems the analog waveforms need only to be captured as snap shots and continuous digitisation is not necessary. Such applications include pulse echo phenomena (radar, ultrasonics), pulse shape recording (high energy physics experiments), and laboratory instrumentation (oscilloscopes, transient digitisers). In these applications an input waveform can be sampled at a high sampling frequency for a limited period of time, and the samples are stored in an analog memory. The analog samples are then retrieved at a lower rate and digitised with a slow analog-to-digital (ADC) converter before a new waveform is acquired. Advantages of using an analog memory include low overall power dissipation and cost, high density, and potentially superior dynamic range at high sampling rates.

A block diagram of a typical waveform acquisition system is shown in Figure 1.1. The electrical signal generated in the detector or sensor is amplified and shaped. The analog waveform is then sampled at high speed rate by using a fast write clock and stored in the analog memory. The stored information is read out at slow rate and is converted into digital form. Because the readout speed and latency are not crucial, a commercial ADC can be used to convert data from analog into digital form. In addition, many signal channels can be multiplexed onto one ADC. The use of an analog memory eases the speed required of the ADC considerably and therefore significantly reduces the cost and the power dissipation.

Specific application for the memories proposed in this work appears for the camera electronics of the Cherenkov telescopes [1] in the High Energy $S$ tereoscopic $S$ ystem (HESS) project [2]. Cameras for these telescopes and their readout systems were developed at Max-Planck-Institut für Kernphysik in Heidelberg. A large part of the trigger electronics, analog signal storage, and monitoring electronics are integrated in the camera electronics of the Cherenkov telescope. Fast photomultipliers (PMTs) are used to convert the Cherenkov light from the sky into electrical signals. The proposed analog memories are an alternative for the camera electronics of the Cherenkov telescopes where continuous data acquisition is not required.


Figure 1.1: Signal acquisition in an analog memory.

A number of concepts and circuits considered in this thesis have been taken from [26] and adapted for the Cherenkov application. This is the case of the analog memory architecture, of the readout operational amplifier and of the control circuits. Changes in the design from [26] can be found in the high speed addressing circuit and read control circuit.

In this thesis the basic characteristics of integrated transistor switches and capacitors are reviewed and two circuits for waveform sampling at rate of 500 MHz are introduced. Each circuit consists of four channels with 128 cells in each channel for acquiring analog waveforms. The architectures of these circuits are investigated in detail with respect to their theoretical dc and ac performances. Both switched capacitor analog memories for capturing fast signals from Cherenkov telescopes have been integrated in the Austria Microsystems (AMS) $0.8 \mu \mathrm{~m}$ complementary metal oxide semiconductor (CMOS) process with poly-to-poly capacitors. The chips have been tested at ASIC laboratory in Heidelberg and the experimental results are presented in this thesis.

### 1.2 Outline

The implementation of analog memory cells using switched capacitor circuits is described in Chapter 2. Several analog memory architectures that have been implemented are examined briefly. The chapter then describes the MOS transistor explored with respect to its use as a voltage switch. The error voltages are evaluated for several memory cell configurations wherein the switch is inserted in the signal or signal return paths. The limiting factors governing the matching of the signal responses among individual memory cells are identified.

Chapter 3 introduces an analog memory core architecture. The operation of this
memory and its expected performance are discussed. Performance parameters such signal range, small signal acquisition bandwidth, and acquisition time are presented. The memory circuit's transfer function is derived, illustrating the effect of component mismatch within a memory channel on the memory response.

The folded cascode amplifier architecture is described in Chapter 4. The amplifier is examined and its gain, bandwidth, and noise are investigated. The simulation results are compared to the calculated parameters.

The control circuits which provide the write and read addresses for analog memory core are described in Chapter 5. A write control circuit comprising delay chains with feedback control circuits is proposed. Depending of the chip version, the read control circuit is implemented with shift registers or decoders.

Calibration and correction procedures that can be used for high precision data acquisition are reviewed in Chapter 6.

The simulation and experimental results of two circuits are presented in Chapter 7. These circuits were integrated in a AMS $0.8 \mu \mathrm{~m}$ CMOS technology with poly-to-poly capacitors. The test setups used for the characterisation of the memories are explained and experimental results are presented. A dynamic range of 8 bits has been achieved for sampling rate of 500 MHz .

Chapter 8 summarises the contributions of this research and identifies areas of future study.

Chapter 1: Introduction

## Chapter 2

## Switched Capacitor Analog Memory Cell

### 2.1 Overview

In this chapter the operation of the MOS transistor is investigated with emphasis on its use in sample and hold configuration. The chapter starts with a short description of some architectures that have been realised in switched capacitor technologies. In the following section the analog memory concept is explained. In Section 2.5 and Section 2.6 are expressed the error voltages for MOS transistors and CMOS transmission gates as a function of the circuit parameters. Implementation of poly-to-poly capacitors for the storage of the sampled signal is reviewed in Section 2.7. For many analog memory applications the uniformity of the memory cell transfer characteristic in a channel is more important than the absolute channel offset and gain. The parameters limiting this uniformity are discussed in Section 2.8.

### 2.2 Analog Memory Architectures

Strong cost and performance incentives especially encourage the use of analog switched capacitor memories in high energy physics experiments [3]. Fast analog waveform capture for thousands of channels must be provided with a minimum of power dissipation. The design challenge is to produce an uniform and linear response in large number of memory cells at a level of performance comparable to the accuracy inherent in the technology. Principal performance issues are cell-to-cell offset and gain variations within a memory channel, which are governed by the circuit architecture and its sensitivity to the matching properties of its constituent transistors and capacitors [4]-[6]. In high precision applications, the lowest achievable cell non-uniformities may not be acceptable and must therefore eliminated by correcting the data. In large systems, it is essential that the number of correction constants and the computational effort to be minimised.

Early analog memory circuits based on a sample and hold topology contain a sampling switch, a storage capacitor, and a readout buffer in each memory cell [7]-[10]. In order to
meet the need for lower power and higher density, architectures based on switched capacitor circuits were introduced [11]-[17]. In these circuits, each channel comprises a bank of capacitors that are switched to a single operational amplifier for readout. Architectures in which the sampling transistors are placed in the signal path [7]-[13] exhibit signal dependent charge injection in each cell. Cell pedestals are then a function of the input signal and may require individual offset, gain, and linearity corrections. In addition, a serious disadvantage of these implementations in high speed applications is the dependence of the sampling transistor turn off time on the signal level [8].

In circuits based on traditional charge redistribution switched capacitor techniques [17], sampling switch charge injection can be made independent of the signal level, but the cell gain is a linear function of the size of the storage capacitor. Cell-to-cell gain matching of better than $0.5 \%$ across an entire channel is therefore difficult to achieve, and both offset and gain corrections are commonly needed for each cell.

An analog memory architecture published in [26] was used in this thesis and described in Chapter 3. It will be shown that for this architecture the memory cell pedestal voltages are independent of the input signal voltage.

### 2.3 Analog Memory Concept

The concept of an analog memory circuit comprising $M$ signal channels with $N$ cells in each channel is shown in Figure 2.1. Each cell of the memory $C_{j, i}$ is located on the column address $i(1 \leq i \leq N)$ and the row address $j(1 \leq j \leq M)$. An analog input signal $V_{i n j}(t)$ is applied to all $N$ memory cells in the channel $j$. The write control signals $w<1>$ through $w<N>$ as well as the read control signals $r<1>$ through $r<N>$ are common to all channels. The analog waveforms are stored in the analog memory by sequentially addressing the memory cells within a channel via the write control signals $w<1>$ through $w<N>$. After the write phase is finished, the readout phase is initiated by applying sequentially the read addresses $r<1>$ through $r<N>$. The analog output $V_{\text {outj }}(t)$ can be digitised by an on or off-chip ADC converter which provides the digital information $V_{\text {outj }}$.

The maximum number of the analog values which can be stored in the array represented in Figure 2.1 is the number of rows $M$ times the number of columns $N$. Usually in analog memory applications $[8,9]$ the number of channels is large compared with the number of cells in one channel $(M \gg N)$. In such applications, the minimum time between the acquisition of two consecutive input waveforms must be long enough to permit a sequential read out of the data.

This thesis focuses on analog waveform sampling applications in which the number of cells in a channel is large compared to the number of channels on one chip ( $N \gg M$ ).

For both types of applications where $(M \gg N)$ and $(N \gg M)$ the time between the readout of two adjacent memory cells can be much larger than the time between the acquisition two consecutive input samples. This facilities the use of a low speed high resolution ADC converter. Generally, a single converter is sufficient for digitisation of the analog waveforms from many memory cells.


Figure 2.1: Simplified representation of an analog memory.

### 2.4 CMOS Technology

The AMS $0.8 \mu \mathrm{~m}$ CMOS process is a twin-well technology on $p$-substrate with double metal and double poly [40]. In a twin-well technology, there are created individual wells for NMOS and PMOS transistors and the substrate may be either $n$-type or $p$-type. The structure of an $n$-channel and $p$-channel MOS transistor using a $n$-well technology is shown in Figure 2.2. The $n$-channel device is formed with two heavily doped $n^{+}$regions diffused into a lighter doped $p$-substrate. The two $n^{+}$regions are called $d$ (drain) and $s$ (source), and are separated by a distance, $L$ (referred to as the device length). At the surface between the drain and source lies a gate electrode $g$ that is separated from the silicon by a thin dielectric material (silicon dioxide). The $b$ terminal is the bulk, or substrate, which contains the drain and source diffusions. Similarly, the $p$-channel transistor is formed by two heavily doped $p^{+}$regions within a lightly doped $n$ for $n$-well processes. It, too, has a gate on the surface between the drain and source separated from the silicon by a thin dielectrical material (silicon dioxide). For a $n$-well process, the $p$-substrate connection is common throughout the integrated circuit and is connected to the lowest potential. Multiple $n$-wells can be fabricated on a single circuit, and they can be connected to different potentials in various ways depending upon the application. Essentially both NMOS and PMOS transistors have four terminals as identified in Figure 2.2 by $g$ (gate), $d$ (drain), $s$ (source) and $b$ (bulk).

An interesting observation can be made from the layout of the MOS transistor in Figure 2.2. The MOS devices are totally geometrically symmetric with respect to drain and source and so must also be electrically symmetric. The designation of drain and source is thus arbitrary. In many applications a convention has evolved for convenience and consistency in device modelling in regard to drain and source designation.


Figure 2.2: Physical structure of an NMOS and PMOS transistor in a $n$-well CMOS technology.

### 2.5 NMOS Transistor Switch

### 2.5.1 NMOS Switch Resistance

In an analog memory cell the MOS transistor can be used as a voltage switch. Two sample and hold configurations were proposed in Figure 2.3 using an NMOS transistor as switch and a storage capacitor $C_{S}$.

An expression of the on channel resistance can be found as follows. In the on state of the switch, the voltage across the switch should be small, and the gate-to-source voltage $V_{G S}$ should be large. Therefore, the NMOS transistor is assumed to be in the ohmic region [18]-[21] $\left(V_{D S}<V_{G S}-V_{T}\right)$ and the current through the device is given by

$$
\begin{equation*}
I_{D S}=\mu_{n} C_{o x} \frac{W}{L}\left(V_{G S}-V_{T}-\frac{V_{D S}}{2}\right) V_{D S} \tag{2.1}
\end{equation*}
$$

where $V_{D S}$ is the drain-to-source voltage, $\mu_{n}$ is the electron mobility in the channel, $W$ and $L$ are the width and length of the channel, $V_{T}$ is the threshold voltage and $C_{o x}$ is the oxide capacitance per unit area. The on resistance of the channel can be approximated by

$$
\begin{equation*}
R_{D S}=\frac{1}{\frac{\partial I_{D S}}{\partial V_{D S}}} \approx \frac{1}{\mu_{n} C_{o x} \frac{W}{L}\left(V_{G S}-V_{T}\right)} \tag{2.2}
\end{equation*}
$$

The on resistance is inversely proportional to the $W$ over $L$ ratio and is nonlinear since it depends on the gate-to-source voltage.


Figure 2.3: NMOS switch placed in (a) signal and (b) signal return path.

### 2.5.2 Error Voltage

As long as the the NMOS switches are conducting, the voltage across the storage capacitor in Figure 2.3 is given by

$$
\begin{equation*}
\Delta V_{s}=V_{i n}-V_{C} \tag{2.3}
\end{equation*}
$$

where $V_{i n}$ is the input voltage and $V_{C}$ is the reference voltage. The NMOS transistor turns off when the gate-to-source voltage is less than the threshold voltage. The voltage across the capacitor after turn off of the sampling switch is

$$
\begin{equation*}
\Delta V_{s}=V_{i n}-V_{C}-V_{p} \tag{2.4}
\end{equation*}
$$

where $V_{p}$ is the pedestal voltage due to charge injection and clock feedthrough effect [22][25]. In Appendix B these effects are explained in detail and the expression of the pedestal voltage for an NMOS switch placed in signal return path is derived. The magnitude of the pedestal voltage differs for the two cell arrangements represented in Figure 2.3.

In the configuration shown in Figure 2.3(a) the pedestal voltage can be derived in similar way than in Appendix B and written as follows

$$
\begin{equation*}
V_{p}=\frac{\alpha C_{o x} W L}{2 C_{S}}\left(V_{H}-V_{i n}-V_{T}\right)+\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}\left(V_{i n}-V_{L}+V_{T}\right) . \tag{2.5}
\end{equation*}
$$

$C_{p}$ is the parasitic capacitance to ground, $C_{o v}$ is the gate overlap capacitance, $\alpha$ is a coefficient $(0<\alpha<1), V_{L}$ and $V_{H}$ are the low and high levels of the transistor gate voltage. The pedestal voltage can be split into a gain error and an offset,

$$
\begin{equation*}
V_{p}=\varepsilon V_{i n}+V_{o f} \tag{2.6}
\end{equation*}
$$

The gain error in the circuit is

$$
\begin{equation*}
\varepsilon=\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}-\frac{\alpha C_{o x} W L}{2 C_{S}} \tag{2.7}
\end{equation*}
$$



Figure 2.4: Pedestal voltage as a function of input voltage for NMOS switch.
while the offset voltage is

$$
\begin{equation*}
V_{o f}=\frac{\alpha C_{o x} W L}{2 C_{S}}\left(V_{H}-V_{T}\right)-\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}\left(V_{L}-V_{T}\right) . \tag{2.8}
\end{equation*}
$$

Following (2.5) through (2.8) for the circuit configuration shown in Figure 2.3(a), the error voltage $V_{p}$ during turn off depends on the input signal level.

The circuit shown in Figure 2.3(b) can be analysed in the same manner as the circuit in Figure 2.3(a), with the result that the pedestal voltage (see Appendix B) is for this configuration

$$
\begin{equation*}
V_{p}=-\frac{\alpha C_{o x} W L}{2 C_{S}}\left(V_{H}-V_{C}-V_{T}\right)-\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}\left(V_{C}-V_{L}+V_{T}\right) . \tag{2.9}
\end{equation*}
$$

The gain error and offset voltage can be written as

$$
\begin{gather*}
\varepsilon=0  \tag{2.10}\\
V_{o f}=-\frac{\alpha C_{o x} W L}{2 C_{S}}\left(V_{H}-V_{C}-V_{T}\right)-\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}\left(V_{C}-V_{L}+V_{T}\right) . \tag{2.11}
\end{gather*}
$$

It is evident from (2.9) through (2.11) that the error voltage is independent on the input signal voltage.

The results of SPICE [43]-[46] simulations for the two circuits in Figure 2.3 when they are implemented in the AMS $0.8 \mu \mathrm{~m}$ CMOS technology are illustrated in Figure 2.4. The


Figure 2.5: Timing errors when the sampling switch is placed in signal path.
absolute values of the simulated pedestal voltages are plotted as a function of the input voltage. The $W / L$ ratio of the NMOS transistor was set to $25 \mu \mathrm{~m} / 0.8 \mu \mathrm{~m}$ and the size of the sampling capacitance was 500 fF . The gate voltage was a ramp which fell from the high value 5 V toward the low value 0 V in 300 ps . The pedestal voltage varies by 40 mV across an input voltage range of 2 V when the switch is inserted in signal path (Figure 2.3(a)) or is constant (Figure 2.3(b)).

### 2.5.3 Distortion and Timing Errors

In the preceding subsection the responses of two sample and hold cells to dc input signals were evaluated. This subsection proposes an analysis of distortion and timing errors for ac input signals.

For the configuration shown in Figure 2.3(a) an ac input pulse with an amplitude of $A_{i n}$ and rise and fall times of $t_{i n r}$ was considered. The process is illustrated in Figure 2.5. The gate control voltage of the NMOS transistor fell from the high value $V_{H}$ to the low value $V_{L}$ with the fall time of $t_{f}$. At the ideal sampling time $t_{s}$ the switch is supposed turned off at high level $V_{H}$ of the gate control voltage. In reality, the switch turns off when the gate control voltage reaches $\left(V_{i n}+V_{T}\right)$ and the actual sampling time $t_{s}^{\prime}$ is given by

$$
\begin{equation*}
t_{s}^{\prime}=t_{s}+\frac{t_{f}}{V_{H}-V_{L}}\left(V_{H}-V_{i n}-V_{T}\right) \tag{2.12}
\end{equation*}
$$

For the rising input signal when

$$
\begin{equation*}
V_{i n}=\frac{A_{i n}}{t_{i n r}} t \tag{2.13}
\end{equation*}
$$



Figure 2.6: Timing errors when the sampling switch is placed in signal return path.
the output signal after changing the time scale can be written as follows

$$
\begin{equation*}
V_{o u t}=\frac{A_{\text {in }}}{t_{i n r}}\left[t+\frac{t_{f}}{V_{H}-V_{L}}\left(V_{H}-V_{\text {in }}-V_{T}\right)\right] . \tag{2.14}
\end{equation*}
$$

Inserting (2.13) into (2.14), the dependence $d V_{\text {out }} / d t$ on $d V_{\text {in }} / d t$ can be expressed as

$$
\begin{equation*}
\frac{d V_{\text {out }}}{d t}=\left(1-\frac{A_{i n}}{t_{i n r}} \frac{t_{f}}{V_{H}-V_{L}}\right) \frac{d V_{\text {in }}}{d t} \tag{2.15}
\end{equation*}
$$

The ratio $A_{i n} / t_{i n r}$ is positive for a rising input signal and negative for a falling input signal. The resulting signal slope $d V_{\text {out }} / d t$ is smaller for rising input signals and larger for falling signals, as indicated with dashed lines in Figure 2.5. The sample and hold configuration wherein the switch is inserted in the signal path introduces timing errors and signal distortion.

For sinusoidal input signals, $V_{\text {in }}=A_{\text {in }} \sin (2 \pi f t)$, the output waveform $V_{\text {out }}$ is given by

$$
\begin{equation*}
V_{\text {out }}=A_{\text {in }} \sin \left\{2 \pi f\left[t+\frac{t_{f}}{V_{H}-V_{L}}\left(V_{H}-V_{T}\right)-\frac{A_{\text {in }} t_{f}}{V_{H}-V_{L}} \sin (2 \pi f t)\right]\right\} . \tag{2.16}
\end{equation*}
$$

The output result is an analog waveform which is harmonic distortioned in comparison with the input signal.

For the circuit of Figure 2.3(b), where the sampling switch is placed in the signal return path, the actual sampling time is given by

$$
\begin{equation*}
t_{s}^{\prime}=t_{s}+\frac{t_{f}}{V_{H}-V_{L}}\left(V_{H}-V_{C}-V_{T}\right), \tag{2.17}
\end{equation*}
$$

as illustrated in Figure 2.6. In the same manner can be determined

$$
\begin{equation*}
\frac{d V_{o u t}}{d t}=\frac{d V_{i n}}{d t} \tag{2.18}
\end{equation*}
$$

and for sinusoidal input signals, $V_{i n}=A_{i n} \sin (2 \pi f t)$,

$$
\begin{equation*}
V_{\text {out }}=A_{\text {in }} \sin \left\{2 \pi f\left[t+\frac{t_{f}}{V_{H}-V_{L}}\left(V_{H}-V_{C}-V_{T}\right)\right]\right\} . \tag{2.19}
\end{equation*}
$$

Thus, there is a constant time delay for pulse inputs and a constant phase shift for input sine waves. As a conclusion, the circuit in Figure 2.3(b) exhibits superior performance in respect to amplitude and timing errors.

### 2.6 CMOS Transmission Gate Switch

The CMOS transmission gate simply consists of a complementary pair of MOS transistors connected in parallel. In comparison with MOS transistors, the CMOS transmission gates require the generation of complementary control signals, which could be difficult to implement in high speed sampling circuits. In the following subsection the error voltage terms for the complementary switch are described.

### 2.6.1 CMOS Switch Resistance

In Figure 2.7 is represented a basic sample and hold configuration of a CMOS transmission gate switch placed in signal path. The on resistances of the NMOS and PMOS transistors are

$$
\begin{align*}
& R_{D S n}=\frac{1}{\frac{\partial I_{D S n}}{\partial V_{D S n}}} \approx \frac{1}{\mu_{n} C_{o x} \frac{W_{n}}{L_{n}}\left(V_{G S n}-V_{T n}\right)}  \tag{2.20}\\
& R_{D S p}=\frac{1}{\frac{\partial I_{D S p}}{\partial V_{D S p}}} \approx \frac{1}{\mu_{p} C_{o x} \frac{W_{p}}{L_{p}}\left(-V_{G S p}+V_{T p}\right)} \tag{2.21}
\end{align*}
$$

where $\mu_{p}$ is the hole mobility. The conductance of the complementary CMOS switch is simply the sum of the individual NMOS and PMOS conductances

$$
\begin{equation*}
\frac{1}{R_{D S}}=\frac{1}{R_{D S n}}+\frac{1}{R_{D S p}} \tag{2.22}
\end{equation*}
$$

With $V_{G S n}=V_{G n}-V_{i n}, V_{G S p}=V_{G p}-V_{i n}$, and $V_{T n}=-V_{T p}=V_{T}$, this equation can be rewritten as

$$
\begin{array}{r}
\frac{1}{R_{D S}} \approx\left(\mu_{p} \frac{W_{p}}{L_{p}}-\mu_{n} \frac{W_{n}}{L_{n}}\right) C_{o x} V_{i n}+ \\
+\mu_{n} C_{o x} \frac{W_{n}}{L_{n}}\left(V_{G n}-V_{T}\right)+\mu_{p} C_{o x} \frac{W_{p}}{L_{p}}\left(-V_{G p}-V_{T}\right) . \tag{2.23}
\end{array}
$$



Figure 2.7: Schematic of the CMOS switch placed in signal path.

The conductance of the transmission gate depends on the input signal level as expressed in (2.23). However, the first term in this equation can be eliminated by choosing the width over length ratios of the transistors according to their mobility ratio

$$
\begin{equation*}
\frac{W_{n}}{L_{n}}=\left(\frac{\mu_{p}}{\mu_{n}}\right) \frac{W_{p}}{L_{p}} \tag{2.24}
\end{equation*}
$$

In practice, a fraction of the input level dependence will remain since the ratio of the mobilities can not be accurately controlled in the fabrication process.

### 2.6.2 Error Voltage

It is assumed that both transistors NMOS and PMOS turn off simultaneously and therefore the error voltages can be summed. For the circuit configuration in Figure 2.7 the voltage $\Delta V_{s}$ across the storage capacitor becomes

$$
\begin{equation*}
\Delta V_{s}=V_{i n}-V_{C}-V_{p} \tag{2.25}
\end{equation*}
$$

with

$$
\begin{equation*}
V_{p}=V_{p n}+V_{p p} \tag{2.26}
\end{equation*}
$$

where $V_{p n}$ and $V_{p p}$ are pedestal voltages for NMOS and PMOS transistors due to charge injection and clock feedthrough effect. The error voltage $V_{p n}$ can be written as in (2.5)

$$
\begin{equation*}
V_{p n}=\frac{\alpha C_{o x} W_{n} L_{n}}{2 C_{S}}\left(V_{H}-V_{i n}-V_{T}\right)+\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}\left(V_{i n}-V_{L}+V_{T}\right) \tag{2.27}
\end{equation*}
$$

and the error voltage $V_{p p}$ can be derived in a similar fashion to that for the NMOS transistor with the following result:

$$
\begin{equation*}
V_{p p}=-\frac{\alpha C_{o x} W_{p} L_{p}}{2 C_{S}}\left(V_{i n}-V_{L}-V_{T}\right)-\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}\left(V_{H}-V_{i n}+V_{T}\right) \tag{2.28}
\end{equation*}
$$

The total pedestal error voltage $V_{p}$ is

$$
\begin{array}{r}
V_{p}=\left[\frac{2 C_{o v}}{C_{o v}+C_{S}+C_{p}}-\frac{\alpha C_{o x}}{2 C_{S}}\left(W_{n} L_{n}+W_{p} L_{p}\right)\right] V_{i n}+ \\
+\frac{\alpha C_{o x}}{2 C_{S}}\left[W_{n} L_{n}\left(V_{H}+V_{L}\right)+\left(W_{p} L_{p}-W_{n} L_{n}\right) V_{T}\right]-\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}\left(V_{H}+V_{L}\right) . \tag{2.29}
\end{array}
$$

The total pedestal voltage can be split into the gain error $\varepsilon$ and offset voltage $V_{o f}$,

$$
\begin{equation*}
V_{p}=\varepsilon V_{i n}+V_{o f} . \tag{2.30}
\end{equation*}
$$

Minimum error voltage in (2.29) is achieved for equivalent areas of both transistors

$$
\begin{equation*}
W_{n} L_{n}=W_{p} L_{p} \tag{2.31}
\end{equation*}
$$

Under this condition the pedestal voltage becomes

$$
\begin{gather*}
V_{p}=\left(\frac{2 C_{o v}}{C_{o v}+C_{S}+C_{p}}-\frac{\alpha C_{o x} W_{n} L_{n}}{C_{S}}\right) V_{i n}+ \\
+\frac{\alpha C_{o x} W_{n} L_{n}}{2 C_{S}}\left(V_{H}+V_{L}\right)-\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}\left(V_{H}+V_{L}\right) \tag{2.32}
\end{gather*}
$$

and the gain error and offset voltage are

$$
\begin{gather*}
\varepsilon=\frac{2 C_{o v}}{C_{o v}+C_{S}+C_{p}}-\frac{\alpha C_{o x} W_{n} L_{n}}{C_{S}}  \tag{2.33}\\
V_{o f}=\frac{\alpha C_{o x} W_{n} L_{n}}{2 C_{S}}\left(V_{H}+V_{L}\right)-\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}\left(V_{H}+V_{L}\right) . \tag{2.34}
\end{gather*}
$$

The pedestal voltages introduced in the circuit shown in Figure 2.8 can be written for NMOS transistor as in (2.9)

$$
\begin{equation*}
V_{p n}=-\frac{\alpha C_{o x} W_{n} L_{n}}{2 C_{S}}\left(V_{H}-V_{C}-V_{T}\right)-\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}\left(V_{C}-V_{L}+V_{T}\right) \tag{2.35}
\end{equation*}
$$

and for PMOS transistor as

$$
\begin{equation*}
V_{p p}=\frac{\alpha C_{o x} W_{p} L_{p}}{2 C_{S}}\left(V_{C}-V_{L}-V_{T}\right)+\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}\left(V_{H}-V_{C}+V_{T}\right) \tag{2.36}
\end{equation*}
$$



Figure 2.8: Schematic of the CMOS switch placed in signal return path.

The total pedestal voltage $V_{p}$ is the sum of the individual contributions as in (2.26)

$$
\begin{array}{r}
V_{p}=\frac{\alpha C_{o x}}{2 C_{S}}\left[W_{p} L_{p}\left(V_{C}-V_{L}\right)-W_{n} L_{n}\left(V_{H}-V_{C}\right)+\left(W_{n} L_{n}-W_{p} L_{p}\right) V_{T}\right]+ \\
+\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}\left(V_{H}+V_{L}-2 V_{C}\right) \tag{2.37}
\end{array}
$$

and is independent of the input signal level. Under the condition that $W_{n} L_{n}=W_{p} L_{p}$ for the circuit simplifies to

$$
\begin{equation*}
V_{p}=\frac{\alpha C_{o x} W_{n} L_{n}}{2 C_{S}}\left(2 V_{C}-V_{L}-V_{H}\right)+\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}\left(V_{H}+V_{L}-2 V_{C}\right) \tag{2.38}
\end{equation*}
$$

Thus the gain error and offset voltage become

$$
\begin{gather*}
\varepsilon=0  \tag{2.39}\\
V_{o f}=\frac{\alpha C_{o x} W_{n} L_{n}}{2 C_{S}}\left(2 V_{C}-V_{L}-V_{H}\right)+\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}\left(V_{H}+V_{L}-2 V_{C}\right) . \tag{2.40}
\end{gather*}
$$

As is the case for a single transistor switch, the circuit configuration with the switch in the signal path has a pedestal voltage that is dependent on the input signal voltage (2.32), whereas $V_{p}$ is constant when the switch is inserted in the signal return path (2.38).

In this subsection it was assumed that the two complementary switches turn off simultaneously and part of the injected channel charge thus cancels. In practice, this is hard to accomplish, and the error voltages may be larger than suggested by (2.32) and (2.38). An important remark is that the gain error of the CMOS transmission gate is larger than the gain error of the MOS transistor when the switches are placed in signal path.


Figure 2.9: Pedestal voltage as a function of input voltage for CMOS switch.

The optimum performance for a CMOS transmission gate can be achieved using (2.24) and (2.31) to determine the geometry of the transistors. These relations give

$$
\begin{equation*}
L_{n}=L_{p} \sqrt{\frac{\mu_{n}}{\mu_{p}}} \tag{2.41}
\end{equation*}
$$

and

$$
\begin{equation*}
W_{p}=W_{n} \sqrt{\frac{\mu_{n}}{\mu_{p}}} . \tag{2.42}
\end{equation*}
$$

For AMS $0.8 \mu \mathrm{~m}$ CMOS technology the mobilities are listed in Table A. 1 of Appendix A and therefore (2.41) and (2.42) can be rewritten as

$$
\begin{equation*}
L_{n} \approx 1.665 L_{p} \tag{2.43}
\end{equation*}
$$

and

$$
\begin{equation*}
W_{p} \approx 1.665 W_{n} \tag{2.44}
\end{equation*}
$$

The two circuits in Figure 2.7 and Figure 2.8 have been implemented in AMS $0.8 \mu \mathrm{~m}$ CMOS technology and simulated with SPICE. The values of the pedestal voltages are plotted as a function of the input voltage and the results are shown in Figure 2.9. The storage capacitor was 500 fF . $W_{n}$ and $L_{p}$ were set to $25 \mu \mathrm{~m}$ and $0.8 \mu \mathrm{~m}$, respectively. $L_{n}$ and $W_{p}$ were calculated from (2.43) and (2.44) with the values $1.33 \mu \mathrm{~m}$ and $41.6 \mu \mathrm{~m}$. The gate voltages were two ramps of 300 ps each one. For an input voltage range of 2 V , the pedestal voltage varies by 140 mV when the switch is inserted in signal path (Figure 2.7), or is constant for the alternative configuration (Figure 2.8).

## Parallel-Plate Capacitors Polysilicon-Oxide-Polysilicon



- Linear capacitors; absolute value difficult to control;
- Poly-poly capacitors can be matched to within $0.1 \%-1 \%$.
- special layout considerations must be given to achieve the lower matching figure ( $0.1 \%$ )
- Not always available in digital CMOS process

Good temperature characteristics.

Figure 2.10: Physical structure of poly-to-poly capacitor.

### 2.7 Capacitors

The quality of capacitors determines the performance of an analog memory. Important issues are the matching of nominally identical capacitors and the absolute sizes and matching of associated parasitic capacitances. There are basically three types of capacitors suitable for analog circuit design available in CMOS processes: poly-over-diffusion capacitors, metal-to-metal capacitors and poly-to-poly capacitors. The first type of capacitor is formed using a polysilicon layer on top of crystalline silicon separated by a dielectric (silicon dioxide layer). In order to achieve a low voltage coefficient capacitor, the bottom plate must be heavily doped diffusion, which generally requires an extra implantation step in the fabrication process. The second type of capacitor is that formed by two metal layers separated by a dielectric. The advantages of this capacitor are its low voltage dependence and a good temperature characteristic. Finally, the third type of capacitor consists of two polysilicon layers separated by silicon dioxide, as illustrated in Figure 2.10. It can be seen that a double polysilicon process is needed to implement this capacitor since both the upper and lower plates are formed with polysilicon. The dielectric is formed by a thin silicon dioxide layer which can only be produced by using several steps beyond the usual single polysilicon process. The advantages of this capacitor are nearly voltage independent parasitic capacitance, good matching (up to $1 \%$ ) and a good temperature characteristic. A typical value for the capacitance in AMS $0.8 \mu \mathrm{~m}$ CMOS technology with poly-to-poly capacitors is $1.77 \mathrm{fF} / \mu \mathrm{m}^{2}$, while the associated bottom plate parasitic capacitance is $0.066 \mathrm{fF} / \mu \mathrm{m}^{2}$ [40].

### 2.8 Matching Properties of Memory Cell

In analog memory applications the uniformity of the memory cell response in one channel is more important than the absolute channel gain and offset. The uniformity is affected by two principal sources of error: inaccuracies in the fabrication process [4]-[6] and control signal feedthrough.

The analog memory cells are designed with the geometry identically but the imperfections in the fabrication process determine a mismatching degree from cell to cell. In addition, there are variations in the area of the storage capacitor plates and the thickness of the dielectric. The characterisation of mismatch in MOS transistors is more complex than that in the case of capacitors. The matching of transistor characteristics on a chip is determined by the matching of threshold voltages, mobilities, oxide and gate overlap capacitances, and the widths and lengths of the transistor gates. The main contribution to cell response variations within a memory channel is the mismatch in the charge injection during turn off of the switch.

Assuming that the variations in width $\delta W$ and length $\delta L$ of two mismatched transistors in a channel are equal $\delta W=\delta L=\delta P$ then

$$
\begin{equation*}
\delta(W L)=(W+\delta P)(L+\delta P)-W L \approx(W+L) \delta P, \tag{2.45}
\end{equation*}
$$

where $\delta(W L)$ is the variation in area. For the circuit configuration in Figure 2.3(b) the pedestal voltage due to the charge injection from (2.9) is

$$
\begin{equation*}
V_{p 1}=-\frac{\alpha C_{o x} W L}{2 C_{S}}\left(V_{H}-V_{C}-V_{T}\right) . \tag{2.46}
\end{equation*}
$$

The variation in pedestal voltage $\delta V_{p 1}$ can be written as

$$
\begin{equation*}
\delta V_{p 1}=-\frac{\alpha C_{o x} \delta(W L)}{2 C_{S}}\left(V_{H}-V_{C}-V_{T}\right) . \tag{2.47}
\end{equation*}
$$

Inserting (2.45) in (2.47) yields

$$
\begin{equation*}
\delta V_{p 1} \approx-\frac{\alpha C_{o x}(W+L) \delta P}{2 C_{S}}\left(V_{H}-V_{C}-V_{T}\right) \tag{2.48}
\end{equation*}
$$

The variation in error voltage due to the nonuniform charge injection $\delta V_{p 1}$ is thus proportional to the channel width and length of the sampling transistor.

The time constant $\tau$ with which the voltage across $C_{S}$ follows a change in the input voltage depends on the on resistance $R_{D S}$ of the sampling switch and the size of the capacitor,

$$
\begin{equation*}
\tau=R_{D S} C_{S} \tag{2.49}
\end{equation*}
$$

If it is assumed that $W \gg L,(2.2)$ and (2.48) are inserted into (2.49), the time constant $\tau$ can be approximated as

$$
\begin{equation*}
\tau \approx-\frac{\alpha L \delta P}{2 \mu_{n} \delta V_{p 1}} \tag{2.50}
\end{equation*}
$$

Thus, switches with smaller $W / L$ ratio yield smaller pedestal mismatches but limit the signal bandwidth of the sampling cell.

In some analog memory applications CMOS transmission gates are used as switches because their absolute pedestal voltages reduced, as discussed in Section 2.6. However, the use of CMOS switches does not improve the matching of the sampling cell performance, since the pedestal error voltages $\delta V_{p 1}$ of the PMOS and NMOS transistors are independent and the resulting pedestal error is therefore not cancelled. If the mismatch of the PMOS and NMOS transistors is uncorrelated, the total error voltage is then given by the square root of the sum of the squares of the individual error voltages.

Another potential source of charge injection mismatch is the variation in sampling capacitance. If $\delta C_{S}$ is the variation in the sampling capacitance, the voltage error $\delta V_{p 1}$ from charge injection onto mismatched capacitors can be written as

$$
\begin{equation*}
\delta V_{p 1} \approx-\frac{\alpha C_{o x} W L}{2 C_{S}}\left(\frac{\delta C_{S}}{C_{S}}\right)\left(V_{H}-V_{C}-V_{T}\right) \tag{2.51}
\end{equation*}
$$

Typically, this error is small compared to the error from the mismatch of the sampling switches and can therefore be neglected.

The second principal source of error is the feedthrough of control signals via the substrate and parasitic inter-layer capacitances. In analog memories, the input waveform is sampled sequentially onto a bank of memory cells. The capacitive coupling from control signal lines to individual memory cell nodes may not be uniform across the chip and therefore the layout of the circuit must be carefully designed to minimise coupling through parasitic inter-layer capacitances and through the substrate. In addition, perturbations in the power supply, ground, signal, buses can be the cause of memory cell performance mismatch, since the signal is captured at different times in the memory cells of the channel.

### 2.9 Summary

The MOS transistors make one of the best switch realisations available in integrated circuit form. They require small area, dissipate very little power, and provide zero offset, low on resistance and high off resistance. Together with storage capacitors, the NMOS transistors create basic sample and hold circuits necessary for acquiring analog waveforms. A voltage switch can be realised by a single NMOS or PMOS transistor, or with a CMOS transmission gate. One of the most serious limitations of the MOS switches is that error voltages are introduced due to the charge injection and clock feedthrough effect. The CMOS transmission gate shows a lower absolute error voltage when compared to a single MOS transistor. The clock circuitry for CMOS switches is more complex because of the requirement for a complementary clock which may be difficult to implement in high speed analog circuits. In addition, it is more important to have an uniformity of the individual memory cell responses in one channel than the absolute error voltage. Therefore the use of a MOS transistor as voltage switch in place of a CMOS transmission gate is suitable to assure an uniformity in the channel.

In a sample and hold circuit the voltage switch can be inserted in signal path or in signal return path. The error voltage is independent of the input signal level when the switch is placed in signal return path and can therefore be cancelled by a simple subtraction procedure. Furthermore, the sample and hold configuration wherein the switch is placed in signal return path introduces a constant time delay for ac input signals.

The analysis of sample and hold configurations presented in this chapter provides basic ideas for the design of analog memory circuits, as proposed in the following chapter.

## Chapter 3

## Analog Memory Circuit

### 3.1 Overview

In this chapter an analog memory circuit for use in high speed data acquisition systems has been introduced. A circuit implementation of the architecture and its theoretical performance are investigated in detail. A short description of the architectures of two chips implemented is presented in Section 3.2. The architecture of the analog memory core is identical for both chips implemented and is described in detail in the following section. The performances of the analog memory are evaluated through a theoretical analysis of dc transfer function, signal range, small signal acquisition bandwidth, acquisition time and leakage current.

### 3.2 Chips Architecture

Two chips for camera electronics of the Cherenkov telescope have been integrated in the Austria Microsystems (AMS) $0.8 \mu \mathrm{~m}$ complementary metal oxide semiconductor (CMOS) process with poly-to-poly capacitors. In Table 3.1 are presented the architectures for both chips. The write control circuit as well as the analog memory core are identically for both chips while the read control circuit is different. The analog memory core is described in detail in the following section and the write and read control circuits are discussed in Chapter 5. FASTSAMP-EV was the first experimental chip implemented followed by FASTSAMP-V1 which is more approached to the camera electronics requirements of the Cherenkov telescope.

The block diagrams of the chips are shown in Figure 3.1. The analog input signals are AnalogInputCh1 through AnalogInputCh4 while the analog outputs are AnalogOutputCh1 through AnalogOutputCh4. The analog waveforms applied at the four inputs are sampled and stored in the analog memory core which consists of four channels with 128 cells in each channel. The write address signals $w<1>$ through $w<128>$ are generated in the high speed write control circuit implemented to achieve 500 MHz sampling frequency. The read address signals $r<1>$ through $r<128>$ are generated in the read control circuit which operates at 100 kHz readout frequency. The

| Chip Name |  | FASTSAMP-EV <br> (Fast Sampling <br> Transmission Recorder <br> - Experimental Version) | FASTSAMP-V1 <br> (Fast Sampling <br> Transmission Recorder <br> - First Version) |
| :---: | :---: | :---: | :---: |
| Architectures | Analog <br> Memory <br> Core | - 4 channels with 128 memory cells in each channel was proposed for acquiring analog waveforms |  |
|  | Write Control Circuit | - sampling rate of 500 MHz <br> - consists of four 32 cell delay chains |  |
|  | Read Control Circuit | - implemented with 4 two-phase shift registers | - implemented with a 1 of 128 decoder |
|  |  | - readout frequency of 100 | kHz |

Table 3.1: Architectures for both chips.
other signals which appear in the block diagrams are provided externally.
The two control signals ComIn and ComOut which appear in the block diagram of FASTSAMP-EV chip in Figure 3.1(a) have been replaced by a single external signal ComInOut necessary for FASTSAMP-V1 chip, as illustrated in Figure 3.1(b). Internally, this replacement has been done by using an inverter.

### 3.3 Analog Memory Core

### 3.3.1 Architecture

The proposed architecture of one channel of the analog memory core [26] is shown in Figure 3.2. $V_{B}$ and $V_{C}$ are dc reference voltages. The operation of the analog memory channel can be described into write and read phases. During the write phase, the switches $S_{i n}$ and $S_{\text {reset }}$ are closed while $S_{\text {out }}$ and read switches $S_{r 1}$ through $S_{r 128}$ are open. The input waveform is then sampled and stored on the storage capacitors $C_{1}$ through $C_{128}$ by sequentially closing and opening the write switches $S_{w 1}$ through $S_{w 128}$. After the analog input waveform has been stored, the switch $S_{i n}$ is opened and $S_{\text {out }}$ is closed. The analog waveform recorded can be read out by consecutively closing and opening the read switches $S_{r 1}$ through $S_{r 128}$.

The architecture presented in Figure 3.2 with a single readout amplifier offers a low power dissipation, small area, and minimum cell-to-cell variations. The use of independent write and read address switches for each cell simplifies the write and read control circuits considerably. As suggested in Chapter 2, the write switches are inserted in the signal return path. The capacitors are switched across the amplifier during readout in order to obtain a cell gain that is insensitive to the size of the sampling capacitor. The description and operation of the architecture shown in Figure 3.2 are analysed in the following subsections.


Figure 3.1: Block diagram for (a) FASTSAMP-EV and (b) FASTSAMP-V1 chips.


Figure 3.2: Memory architecture with one amplifier per channel.


Figure 3.3: Simplified schematic of one analog memory channel.

### 3.3.2 Description

A simplified schematic of one channel of the proposed analog memory [27, 28], comprising 4 blocks of 32 cells, is shown in Figure 3.3. Each memory cell consists of a large write transistor $M_{w i}$, a minimum size read transistor $M_{r i}$, and a sampling capacitor $C_{i}$. The cells are addressed via write lines $w<1>$ through $w<128>$ and read lines $r<1>$ through $r<128>$. The voltage $V_{C}$ is a dc reference common to the sources of all write transistors, $M_{w i}$. The switch $M_{r e s e t}$ serves to configure the operational amplifier as


Figure 3.4: Timing diagram for (a) write and (b) read phases.
a voltage follower in order to force the nodes of the amplifier input and output to the dc bias level $V_{B}$ during reset.

The channel dimensions of the NMOS and PMOS transistors comprising the input switch $M_{i n}$ are $W / L=600 \mu \mathrm{~m} / 1.3 \mu \mathrm{~m}$ and $W / L=999.2 \mu \mathrm{~m} / 0.8 \mu \mathrm{~m}$, respectively. As suggested by (2.41) through (2.44), the relative sizes of these devices were chosen so as to minimise the signal dependence of the switch on resistance and the total error voltage. The drawn dimensions of the write and read transistors are $W / L=25 \mu \mathrm{~m} / 0.8 \mu \mathrm{~m}$ and $W / L=2 \mu \mathrm{~m} / 0.8 \mu \mathrm{~m}$ (minimum size), respectively. The storage capacitor was chosen of 500 fF and the output amplifier is a folded cascode design of the type described in Chapter 4.

The operation of the circuit can be described into write and read cycles. In the write phase, analog signals applied at the channel input, $V_{i n}$, are sampled and stored in the memory cells at a high rate. The stored analog information is subsequently read out serially at the channel output, $V_{o}$, at a lower speed.

During the write phase, the switch $M_{i n}$ is turned on, connecting the signal $V_{i n}$ to the input bus, while the switch $M_{o u t}$ and the read switches $M_{r 1}$ through $M_{r 128}$ are all off,


Figure 3.5: Analog memory channel with parasitic capacitances.
isolating the input bus from the read bus. The switch $M_{\text {reset }}$ is on to keep the read bus at a defined potential $V_{B}=V_{C}=2.5 \mathrm{~V}$ during the entire write phase. An analog signal applied at the circuit's input is sampled onto the cell capacitors $C_{i}$ by sequentially turning transistors $M_{w 1}$ through $M_{w 128}$ on and off, as illustrated in Figure 3.4(a). Samples of the input waveform at 128 discrete times are thereby stored in the memory channel.

The voltage $\Delta V_{s i}$ stored across the capacitor $C_{i}$ in the memory cell $i, 1 \leq i \leq 128$, is after the sampling

$$
\begin{equation*}
\Delta V_{s i}=V_{i n}-V_{C}-V_{p w i} \tag{3.1}
\end{equation*}
$$

where $V_{p w i}$ is the voltage error due to the charge injection and clock feedthrough effect in the switch $M_{w i}$ during turn off. As derived in Appendix B, with the source and drain terminals of the write transistor at reference voltage $V_{C}$ at turn off, the pedestal voltage $V_{p w i}$ can be written as

$$
\begin{align*}
V_{p w i}=-\frac{C_{w i}+\frac{C_{o x} W_{w i} L_{w i}}{2}}{C_{t o t}} \sqrt{\frac{\pi U C_{t o t}}{2 \beta}} \operatorname{erf} & {\left[\sqrt{\frac{\beta}{2 U C_{t o t}}}\left(V_{H}-V_{C}-V_{T}\right)\right]-} \\
& -\frac{C_{w i}}{C_{w i}+C_{p i}+C_{i}}\left(V_{C}-V_{L}+V_{T}\right) \tag{3.2}
\end{align*}
$$

where $C_{w i}$ is the write transistor gate overlap capacitance, $C_{i}$ is the sampling capacitance, $V_{T}$ is the threshold voltage, $V_{L}$ and $V_{H}$ are the low and high levels of the write transistor gate voltage, $C_{o x}$ is the oxide capacitance per unit area, $W_{w i}$ and $L_{w i}$ are the width and length of the write transistor, $U$ is the slew rate of the gate voltage, $C_{p i}$ is the capacitance associated with the cell sampling capacitor terminal connected to the write switch $M_{w i}$,
$\beta=\mu_{n} C_{o x} W_{w i} / L_{w i}$, and $\mu_{n}$ is the electron mobility in the channel. The capacitance $C_{t o t}$ is

$$
\begin{equation*}
C_{t o t}=C_{i}+C_{p i}+C_{w i}+\frac{C_{o x} W_{w i} L_{w i}}{2} \tag{3.3}
\end{equation*}
$$

The important fact of this investigation is that $V_{p w i}$ remains independent of the input voltage, $V_{i n}$.

The parasitic capacitances for one analog memory channel are illustrated in Figure 3.5 and listed in Table A. 2 of Appendix A. The values have been extracted from the layout of the analog memory core which is identically for both chips. The slew rate of the gate voltage $U$ with a typical value of $5 \mathrm{~V} / 300 \mathrm{ps}$ corresponds to the falling edges ( 300 ps ) of the write address signals. The pedestal voltage $V_{p w i}$ has been calculated from (3.2), $V_{\text {pwi }}=-130 \mathrm{mV}$, in which $(-80 \mathrm{mV})$ represents the charge injection contribution and $(-50 \mathrm{mV})$ due to the clock feedthrough effect.

After the write phase has been completed and the input waveform is stored in the analog memory, the read cycle is initiated. During the readout, the switch $M_{i n}$ is turned off while $M_{o u t}$ and $M_{\text {reset }}$ are turned on, forcing both the input bus and the read bus to $V_{B}$. The switch $M_{\text {reset }}$ is then turned off and the voltage stored in the first cell is read out by turning $M_{r 1}$ on as illustrated in Figure 3.4(b). This cycle is repeated for all cells. The input bus must always be forced back to $V_{B}$ before a new cell is read out, otherwise the charge and parasitic capacitances will seriously degrade the circuit's performance. By turning the cell read switches off after the reset switch is turned on, the potential across the capacitors is initialised to nominally 0 V for the next write phase.

### 3.3.3 DC Transfer Function

Once the write switch is turned off, the cell capacitor nodes connected to the cell transistors are left in a high impedance state for the remainder of the write phase and the entire read phase. Therefore the charge at these nodes is conserved and only three parasitic capacitances influence the dc transfer function of a memory cell. One is the capacitance $C_{p i}$, the second parasitic capacitance is the gate overlap capacitance of the read switch, $C_{r i}$, and the third parasitic to be considered is the capacitance, $C_{p p}$, between the inverting input and the output of the amplifier.

The dc transfer function of the memory can be derived using the schematics illustrated in Figure 3.6 and Figure 3.7, which show a memory cell together with the readout amplifier before and after the cell is addressed for readout, respectively. The total charge stored at memory cell node $x_{i}$ in Figure 3.6 after the write transistor $M_{w i}$ is turned off is

$$
\begin{equation*}
Q_{x_{i}}=C_{i}\left(V_{C}+V_{p w i}-V_{i n}\right)+C_{p i}\left(V_{C}+V_{p w i}\right)+C_{r i}\left(V_{C}+V_{p w i}-V_{L}\right) \tag{3.4}
\end{equation*}
$$

The charge $Q_{y_{i}}$ stored at the inverting input node $y_{i}$ of the amplifier before the memory cell is addressed for readout is

$$
\begin{equation*}
Q_{y_{i}}=C_{r i}\left(V_{B}-V_{L}\right) \tag{3.5}
\end{equation*}
$$



Figure 3.6: Circuit configuration before the memory cell is addressed for readout.

After the read switch has been turned on, as illustrated in Figure 3.7, the node $x_{i}$ and node $y_{i}$ are shorted and the total charge is

$$
\begin{equation*}
Q_{x_{i} y_{i}}=Q_{x_{i}}+Q_{y_{i}} \tag{3.6}
\end{equation*}
$$

The charge $Q_{x_{i} y_{i}}$ can be expressed as

$$
\begin{align*}
Q_{x_{i} y_{i}}=\left(C_{i}\right. & \left.+C_{p p}\right)\left(V_{o p m}-V_{o i}\right)+2 C_{r i}\left(V_{o p m}-V_{H}\right)+ \\
& +C_{p i} V_{o p m}-C_{o x} W_{r i} L_{r i}\left(V_{H}-V_{o p m}-V_{T}\right), \tag{3.7}
\end{align*}
$$

where $W_{r i}$ and $L_{r i}$ are the channel width and length of the read transistor. $V_{o p m}$ is the voltage of the inverting input of the amplifier,

$$
\begin{equation*}
V_{o p m}=V_{B}-\frac{V_{o i}-V_{B}}{G} \tag{3.8}
\end{equation*}
$$

and $G$ is the open-loop gain of the amplifier.
When memory cell $i$ is selected for readout, the voltage at the output of the amplifier, $V_{o i}$, can be described as a function of the input voltage $V_{i n}$ in the form

$$
\begin{equation*}
V_{o i}=A_{i} V_{i n}+V_{o f f i} \tag{3.9}
\end{equation*}
$$

where $A_{i}$ is the gain factor and $V_{o f f i}$ is the offset voltage. By solving (3.4) to (3.8), the gain factor $A_{i}$ is

$$
\begin{equation*}
A_{i}=\frac{1}{1+\frac{C_{p p}}{C_{i}}+\frac{1}{G}\left(1+\frac{C_{p p}+C_{p i}}{C_{i}}+\frac{2 C_{r i}}{C_{i}}+\frac{C_{o x} W_{r i} L_{r i}}{C_{i}}\right)} \tag{3.10}
\end{equation*}
$$



Figure 3.7: Circuit configuration when the memory cell is addressed for readout.
and the offset voltage $V_{o f f i}$

$$
\begin{align*}
V_{o f f i}= & V_{B}-\frac{C_{i}}{C_{i}+C_{p p}} V_{C}+\frac{C_{p i}}{C_{i}+C_{p p}}\left(V_{B}-V_{C}\right)-\frac{C_{i}+C_{p i}+C_{r i}}{C_{i}+C_{p p}} V_{p w i}- \\
& -\frac{C_{r i}}{C_{i}+C_{p p}}\left(2 V_{H}-2 V_{L}-V_{B}+V_{C}\right)-\frac{C_{o x} W_{r i} L_{r i}}{C_{i}+C_{p p}}\left(V_{H}-V_{B}-V_{T}\right) . \tag{3.11}
\end{align*}
$$

The sampling capacitance $C_{i}$ can be made large compared to $C_{p p}$ and to $C_{r i}$. Also, the open-loop amplifier gain $G$ is large enough in practical CMOS circuits. With these approximations and supposing that the reference voltage $V_{C}$ is set to the bias voltage $V_{B}$, (3.10) and (3.11) can be rewritten as

$$
\begin{equation*}
A_{i}=\frac{1}{1+\frac{C_{p p}}{C_{i}}} \tag{3.12}
\end{equation*}
$$

and

$$
\begin{equation*}
V_{o f f i}=-\left(1+\frac{C_{p i}}{C_{i}}\right) V_{p w i} . \tag{3.13}
\end{equation*}
$$

Because both $A_{i}$ and $V_{o f f i}$ are independent of the input voltage $V_{i n}$, as indicated by (3.9) to (3.13), it follows that the output voltage of the analog memory $V_{o}$ is a linear function of $V_{i n}$. With the parasitic capacitance values listed in Table A. 2 of Appendix A and $V_{p w i}$ of $(-130 \mathrm{mV})$, the gain cell and offset voltage have been calculated from (3.12) and (3.13) and their values are 0.979 and 141 mV , respectively.

### 3.3.4 Signal Range

Since the cell capacitor nodes connected to the cell transistors remain floating after the write switch is turned off, care must be taken to ensure that no leakage occurs at those nodes, for all possible ac and dc input signals, during the write and read


Figure 3.8: (a) Triangle input waveform. (b) Waveforms at node $x_{i}$ in Figure 3.5 with the write switch turned off at time $t_{1}$ (solid line) and $t_{2}$ (dashed line).
phases. In Figure 3.8(a) is represented a triangle input waveform with a voltage swing of $\Delta V_{i n}=V_{M}-V_{m}$. Shown in Figure 3.8(b) are the waveforms at node $x_{i}$ in Figure 3.5 with the write switch turned off at times $t_{1}$ and $t_{2}$, respectively. The voltage $V_{x_{i}}$ at node $x_{i}$ must not fall below the low level of the gate voltage $V_{L}$ to avoid subthreshold leakage. Therefore $V_{x_{i}} \geq V_{L}$ and the maximum input voltage swing $\Delta V_{i n}$ in the write phase is limited to

$$
\begin{equation*}
\Delta V_{i n} \leq V_{C}-V_{L} \tag{3.14}
\end{equation*}
$$

In the read phase, the maximum voltage swing $\Delta V_{o i}$ at the output of the amplifier must be less than $\left(V_{B}-V_{L}\right)$ to avoid the subthreshold leakage. It follows from (3.9) that the corresponding limit for the input voltage swing during the write phase is then

$$
\begin{equation*}
\Delta V_{i n}=\frac{\Delta V_{o i}}{A_{i}} \leq \frac{V_{B}-V_{L}}{A_{i}} \tag{3.15}
\end{equation*}
$$

### 3.3.5 Small Signal Acquisition Bandwidth

The small signal bandwidth of the analog memory is governed by the impedances of the MOS switches, the size of the sampling capacitance, and the size of associated parasitic capacitances. The equivalent circuit of a memory cell during signal acquisition is shown in Figure 3.9. $R_{w i}$ and $R_{i s}$ represent the write and input switch on resistances. Their values are calculated by (2.2) and (2.20) to (2.22) and given in Table A. 2 of Appendix A.


Figure 3.9: Equivalent circuit of a memory cell during signal acquisition.

In general, the on resistance of the input switch should be low. The capacitance $C_{s}$ is given by

$$
\begin{equation*}
C_{s}=C_{i s}+C_{i n b} \tag{3.16}
\end{equation*}
$$

where $C_{i s}$ is the drain capacitance of the input switch and $C_{i n b}$ is the capacitance between the input bus and ground. The values of these capacitances have been extracted from the analog memory core layout and are also given in Table A.2.

As long as $R_{i s} \ll R_{w i}$ the current $i$ is flowing through $R_{i s}$ and $C_{s}$. Therefore the following transfer functions in Laplace can be written as

$$
\begin{equation*}
\frac{v_{s}}{v_{i n}}(s)=\frac{1}{1-\frac{s}{p_{s}}} \tag{3.17}
\end{equation*}
$$

and

$$
\begin{equation*}
\frac{v_{i}}{v_{s}}(s)=\frac{1}{1-\frac{s}{p_{i}}} \tag{3.18}
\end{equation*}
$$

with $p_{s}=-1 / R_{i s} C_{s}$ and $p_{i}=-1 / R_{w i} C_{i}$. Thus the frequency dependence of the voltage $v_{i}$ across the sampling capacitor $C_{i}$ is given by

$$
\begin{equation*}
\frac{v_{i}}{v_{i n}}(s)=\frac{1}{\left(1-\frac{s}{p_{i}}\right)\left(1-\frac{s}{p_{s}}\right)} \tag{3.19}
\end{equation*}
$$

Because $\left|p_{s}\right|$ is much larger than $\left|p_{i}\right|$, (3.19) can be approximated by a single pole expression

$$
\begin{equation*}
\frac{v_{i}}{v_{i n}}(s) \approx \frac{1}{1-\frac{s}{p_{i}}} \tag{3.20}
\end{equation*}
$$

The cell bandwidth $B$ for the circuit is given by

$$
\begin{equation*}
B=f_{-3 d B}=-\frac{p_{i}}{2 \pi}, \tag{3.21}
\end{equation*}
$$



Figure 3.10: Time response of the analog memory cell to a step input.
where $f_{-3 d B}$ is the -3 dB frequency. The on resistance $R_{w i}$ can be expressed as in (2.2) with $V_{G S}=V_{H}-V_{C}$ and therefore (3.21) becomes

$$
\begin{equation*}
B=\frac{\mu_{n} C_{o x} \frac{W_{w i}}{L_{w i}}\left(V_{H}-V_{C}-V_{T}\right)}{2 \pi C_{i}} . \tag{3.22}
\end{equation*}
$$

For applications where a high input bandwidth is required, the write transistor must be made large because the cell bandwidth $B$ is determined by the size of the sampling capacitor and the resistance of the write transistor.

### 3.3.6 Acquisition Time

The acquisition time is the length of time that the write address switch must stay on in order to acquire a full scale step at the input to a specified accuracy. The small signal transfer function of the analog memory can be approximated by a single pole expression as in (3.20). The circuit response illustrated in Figure 3.10 to a voltage step $v_{i n}(s)=A / s$ at the input is

$$
\begin{equation*}
v_{i}(s)=A\left(\frac{1}{s}-\frac{1}{s-p_{i}}\right) \tag{3.23}
\end{equation*}
$$

The time response to a step input is therefore

$$
\begin{equation*}
v_{i}(t)=A\left(1-e^{p_{i} t}\right) . \tag{3.24}
\end{equation*}
$$

For a given accuracy $\alpha$ in $\%,(3.24)$ can be rewritten as

$$
\begin{equation*}
\frac{\alpha A}{100}=A\left(1-e^{p_{i} t_{a}}\right) \tag{3.25}
\end{equation*}
$$

where $t_{a}$ is the acquisition time. Inserting $p_{i}=-1 / R_{w i} C_{i}$ in (3.25) yields

$$
\begin{equation*}
t_{a}=-R_{w i} C_{i} \ln \left(1-\frac{\alpha}{100}\right) \tag{3.26}
\end{equation*}
$$

For instance, for a given accuracy $\alpha$ of $99 \%, R_{w i}=180 \Omega$ and $C_{i}=500 \mathrm{fF}$, the acquisition time calculated by (3.26) is $t_{a} \approx 415 \mathrm{ps}$. In conclusion, the acquisition time of the analog memory for a given accuracy is less than 0.5 ns .

### 3.3.7 Leakage Current

Leakage currents across drain-bulk and source-bulk $p n$-junctions occur in both PMOS and NMOS transistors. The leakage currents depend of temperature and double for every $8{ }^{\circ} \mathrm{C}$ rise in temperature [26]. At room temperature, a typical value of the leakage current is $I_{l e a k}=15 \mathrm{fA} / \mu \mathrm{m}^{2}$. For the write switch transistor $M_{w i}$ with $W_{w i} / L_{w i}$ ratio of $25 \mu \mathrm{~m} / 0.8 \mu \mathrm{~m}$ the leakage current is $I_{l e a k} W_{w i} L_{w i}(0.3 \mathrm{pA})$. The rate of discharge for a 500 fF storage capacitor $C_{i}$ is then $I_{l e a k} W_{w i} L_{w i} / C_{i}(6 \mu \mathrm{~V} / \mu \mathrm{s})$. The magnitudes of leakage currents are below the nanoampere range, so that they have a negligible effect in the analog memory core.

### 3.4 Summary

In this chapter an analog memory circuit for use in high speed data acquisition systems has been introduced. Each channel in this memory consists of 128 memory cells for storing samples of the input waveform and a single operational amplifier for reading out the stored samples. Each memory cell comprises a storage capacitor, a write switch and a read switch.

The dc transfer function of the analog memory circuit was derived and it was shown that the output voltage is a linear function of the input voltage. In order to achieve a high input bandwidth the write transistors must be made large, which may increase the cell-to-cell response variations. However, in the proposed analog memory architecture the pedestal voltages are not dependent on the input signal level. The pedestal voltage is governed by charge injection and clock feedthrough effect at turn off of the large write switch and a theoretical expression for this voltage is derived in Appendix B.

The main analog memory core has been designed so that the sampling time of the individual memory cells is independent of the input signal level. This removes the need for an extensive ac calibration and sampling time error correction procedures.

## Chapter 4

## Readout Operational Amplifier

### 4.1 Overview

Each channel of the analog memory architecture presented in the previous chapter includes an on-chip operational amplifier which is used during the readout phase. The amplifier must provide sufficient gain, speed, and noise performance for the intended analog memory application. In addition, the noise contribution of the amplifier to the total circuit noise should be small compared to the noise of the analog memory. The folded cascode architecture chosen is simple and attractive because the load capacitance provides the frequency compensation. The amplifier must drive off-chip several picofarads and therefore the stability is assured. The folded cascode amplifier is capable of achieving a high stable loop bandwidth with a large capacitive load. The circuit of the amplifier is described in detail in Section 4.2. In Section 4.3 the folded cascode architecture is examined with respect to gain and bandwidth. Simulation results are presented with the amplifier in both follower and inverting amplifier configurations. In the following section is analysed the total noise including flicker and thermal noise.

### 4.2 Amplifier Circuit

The schematic of the folded cascode amplifier [28] with a $p$-channel differential input pair is shown in Figure 4.1. The circuit comprises a cascade of a common source and a common gate stage. The use of this configuration improves the frequency response and power supply rejection. The small signal impedance at the output node is increased and the voltage gain is simply the product of the transconductance of the input transistors and the impedance of the output node. An important performance advantage of this circuit is that the load capacitance contributes the dominant pole and performs the function of compensation capacitor. The transistors $M_{3}$ and $M_{4}$ operate as current sources and $M_{7}$ through $M_{10}$ operate as an improved Wilson current source. The currents through $M_{3}$ and $M_{4}$ equal the sum of the currents from the differential pair, $M_{1}$ and $M_{2}$, and from the cascode mirror formed by $M_{7}$ through $M_{10}$. The reference voltages $V_{\text {ref } 1}, V_{\text {ref } 2}, V_{\text {bias }}$ are generated by the bias generator formed by the transistors $M_{11}-M_{16}$. The drawn


Figure 4.1: Schematic of the folded cascode amplifier.

| Transistors | Current $[\mu \mathrm{A}]$ | Transconductance $[\mu \mathrm{A} / \mathrm{V}]$ | Conductance [nA/V] |
| :---: | :---: | :---: | :---: |
| $M_{1}, M_{2}$ | 20 | 124.8 | 147.2 |
| $M_{3}, M_{4}$ | 40 | 192.5 | 1130 |
| $M_{5}, M_{6}$ | 20 | 206.7 | 176.9 |
| $M_{7}, M_{8}$ | 20 | 122.3 | 357.4 |
| $M_{9}, M_{10}$ | 20 | 84.12 | 210.3 |

Table 4.1: Dc operating points of MOS transistors.

| Variable | Simulation |
| :---: | :---: |
| $V_{\text {bias }}$ | 3.554 V |
| $V_{\text {ref } 1}$ | 1.242 V |
| $V_{\text {ref } 2}$ | 1.614 V |
| Power Dissipation | $653 \mu \mathrm{~W}$ |

Table 4.2: Simulation results.
dimensions of the channel lengths and widths of MOS transistors are illustrated in Figure 4.1.

The dc voltage gain $G$ of the amplifier $[29,30]$ in Figure 4.1 can be approximated by the product of the transconductance of the input transistor, $g_{m 1}$, and the impedance at the output node, $r_{\text {out }}$,

$$
\begin{equation*}
G \approx g_{m 1} r_{o u t} \approx \frac{g_{m 1}}{\frac{g_{d s 6}\left(g_{d s 2}+g_{d s 4}\right)}{g_{m 6}}+\frac{g_{d s 8} g_{d s 10}}{g_{m 10}}} \tag{4.1}
\end{equation*}
$$

where $g_{d s 2}, g_{d s 4}, g_{d s 6}, g_{d s 8}, g_{d s 10}$ and $g_{m 6}, g_{m 10}$ are conductances and transconductances of the MOS transistors. The dominant pole $p_{1}$ of the circuit is determined by the impedance


Figure 4.2: Amplifier in the (a) voltage follower and (b) inverter configuration.
at the output node together with the output capacitance $C_{\text {out }}$,

$$
\begin{equation*}
p_{1}=\frac{1}{2 \pi r_{\text {out }} C_{\text {out }}} \tag{4.2}
\end{equation*}
$$

where $C_{\text {out }}$ consists of the load capacitance and the parasitic capacitance at the output node.

The dc operating points of the MOS transistors were determined after simulations with SPICE [43]-[46] and listed in Table 4.1. The simulation results for the reference voltages are illustrated in Table 4.2. For a +5 V power supply the power dissipation of the operational amplifier is $653 \mu \mathrm{~W}$. With the values listed in Table 4.1 and Table 4.2, the open loop gain and the output resistance can be calculated from (4.1) and their values are $62828(96 \mathrm{~dB})$ and $503.425 \mathrm{M} \Omega$, respectively. Assuming that for the simulations a 10 pF load capacitance was used, the dominant pole $p_{1}$ calculated from (4.2) is 32 Hz .

### 4.3 Simulation Results

The amplifier was simulated with SPICE in two different configurations in order to investigate performance parameters such as linearity, slew-rate, unity-gain bandwidth and open-loop gain. The schematics of the amplifier connected as a voltage follower and as an inverter are shown in Figure 4.2(a) and (b), respectively. As indicated, the amplifier was evaluated in closed-loop using an operational amplifier $O P 01 B$ [42] provided by AMS $0.8 \mu \mathrm{~m}$ technology library. This CMOS amplifier operates as a buffer and has high input impedance, low offset, high open-loop gain (100 dB) and unity-gain bandwidth of 23 MHz .


Figure 4.3: Upper: Input voltage as a function of output voltage. Lower: Residuals from a fit to a 2.5 V output voltage range. The amplifier is in the inverter configuration.


Figure 4.4: Output voltage plotted as a function of input voltage. The amplifier is in the follower configuration.

The amplifier output voltage range and its linearity were simulated with the amplifier in the inverter configuration, as illustrated in Figure 4.2(b). In Figure 4.3 the input voltage is plotted as a function of the output voltage together with the deviations from a linear fit across a 2.5 V output voltage range. The non-inverting input of the amplifier


Figure 4.5: Amplitude (upper) and phase (lower) plotted as a function of frequency.

| Variable | Simulation | Calculation |
| :---: | :---: | :---: |
| Open-loop gain | 98 dB | 96 dB |
| -3 dB bandwidth | 25 Hz | 32 Hz |
| Unity-gain bandwidth | 1.92 MHz | - |
| Integral linearity | $0.03 \%$ | - |
| Slew-rate | $3.83 \mathrm{~V} / \mu \mathrm{s}$ | - |
| Phase margin | 90 degree | - |
| Output resistance | - | $503.425 \mathrm{M} \Omega$ |
| Equivalent input referred noise @ $\mathrm{f}=100 \mathrm{kHz}$ | $30 \mathrm{nV} / \sqrt{\mathrm{Hz}}$ | $33 \mathrm{nV} / \sqrt{\mathrm{Hz}}$ |

Table 4.3: Simulation and calculation results at 10 pF load capacitance.
was set to 2.5 V . The integral linearity error is the maximum deviation from a linear fit to the output voltage versus the input voltage over the full scale input voltage range, expressed as a percentage of the input voltage range. The calculated non-linearity is $0.03 \%(700 \mu \mathrm{~V} / 2.5 \mathrm{~V})$ over an output voltage range of 2.5 V .

Other amplifier parameters such slew-rate and frequency dependence of the open-loop gain were determined after simulations with the amplifier in the follower configuration. In Figure 4.4 the output voltage is plotted as a function of input voltage with the amplifier in the follower configuration, as shown in Figure 4.2(a). For the simulations it
was assumed that the input transistors are identical (no mismatch), corresponding to a zero offset voltage. The slew-rate of $3.83 \mathrm{~V} / \mu \mathrm{s}$ was calculated after simulations at 10 pF load capacitance. Figure 4.5 shows the open-loop gain and phase represented as a function of frequency. The simulations show an open-loop gain of 98 dB , a phase margin of 90 degree, a unity-gain bandwidth of 1.92 MHz and a -3 dB bandwidth of 25 Hz . For the simulations a 10 pF load capacitance was used, which approximately represents the output load capacitance in the test setups described in Appendix C and Appendix D. This capacitance accounts for the chip package and socket ( 68 pin CLCC), traces on the printed circuit board, and the input capacitance of the AD645 amplifier ( 1 pF ).

The simulations and calculations agree well and are summarised in Table 4.3.

### 4.4 Amplifier Noise

The noise introduced by the amplifier consists of the thermal and the flicker (1/f) noise. The thermal noise is due to random thermal motion of the electron and is independent of the dc current flowing in the component. The flicker noise is associated with carrier traps in the semiconductor which capture and release carriers in a random manner. The spectral noise density for a NMOS transistor [44]-[46] can be written as

$$
\begin{equation*}
S_{f n}(f)=\frac{\overline{v_{t h n}^{2}}+\overline{v_{f n}^{2}}}{\Delta f}=\frac{\overline{i_{t h n}^{2}}+\overline{i_{f n}^{2}}}{g_{m n}^{2} \Delta f}=\frac{8 k T}{3 g_{m n}}+\frac{K_{f n} I_{D S n}^{A_{f n}}}{g_{m n}^{2} C_{o x} W_{n} L_{n} f}, \tag{4.3}
\end{equation*}
$$

where $g_{m n}$ is the transconductance of the transistor, $I_{D S n}$ is the drain-to-source current, $k=1.38 \times 10^{-23}[\mathrm{~J} / \mathrm{K}]$ is the Boltzmann's constant, and $K_{f n}$ and $A_{f n}$ are the flicker noise coefficient and exponent, respectively. In the same manner as for a NMOS transistor, the spectral noise density for a PMOS transistor is given by

$$
\begin{equation*}
S_{f p}(f)=\frac{\overline{v_{t h p}^{2}}+\overline{v_{f p}^{2}}}{\Delta f}=\frac{\overline{i_{t h p}^{2}}+\overline{i_{f p}^{2}}}{g_{m p}^{2} \Delta f}=\frac{8 k T}{3 g_{m p}}+\frac{K_{f p} I_{D S p}^{A_{f p}}}{g_{m p}^{2} C_{o x} W_{p} L_{p} f} . \tag{4.4}
\end{equation*}
$$

The first term in (4.3) or (4.4) represents the thermal noise of the transistor due to the finite resistance of the channel. The second term in (4.3) or (4.4) represents the contribution from the flicker noise.

The input referred thermal noise generated in the folded cascode amplifier is the sum of the statistically independent mean square noise currents from the transistors $M_{1}$ through $M_{10}$. The input referred thermal noise spectral density is then

$$
\begin{equation*}
\frac{\overline{v_{t h}^{2}}}{\Delta f}=\frac{\sum_{j=1}^{10} \overline{i_{t h j}^{2}}}{g_{m 1}^{2} \Delta f}=\frac{\overline{i_{t h 1}^{2}}+\overline{i_{t h 2}^{2}}+\overline{i_{t h 3}^{2}}+\overline{i_{t h 4}^{2}}+\overline{i_{t h 5}^{2}}+\overline{i_{t h 6}^{2}}+\overline{i_{t h 7}^{2}}+\overline{i_{t h 8}^{2}}+\overline{i_{t h 9}^{2}}+\overline{i_{t h 10}^{2}}}{g_{m 1}^{2} \Delta f} \tag{4.5}
\end{equation*}
$$

With matched transistors in each of the pairs $M_{1}-M_{2}, M_{3}-M_{4}, M_{5}-M_{6}, M_{7}-M_{8}$, and $M_{9}-M_{10}$, the input referred thermal noise spectral density for the folded cascode amplifier can be expressed as

$$
\begin{equation*}
\frac{\overline{v_{t h}^{2}}}{\Delta f}=\frac{2\left(\overline{i_{t h 1}^{2}}+\overline{i_{t h 3}^{2}}+\overline{i_{t h 5}^{2}}+\overline{i_{t h 7}^{2}}+\overline{i_{t h 9}^{2}}\right)}{g_{m 1}^{2} \Delta f} \tag{4.6}
\end{equation*}
$$

Inserting the thermal noise terms from (4.3) and (4.4) into (4.6) yields

$$
\begin{equation*}
\frac{\overline{v_{t h}^{2}}}{\Delta f}=\frac{16 k T}{3 g_{m 1}}\left(1+\frac{g_{m 3}+g_{m 5}+g_{m 7}+g_{m 9}}{g_{m 1}}\right) \tag{4.7}
\end{equation*}
$$

The spectral density of the input referred flicker noise generated in the amplifier circuit can be written as

$$
\begin{equation*}
\frac{\overline{v_{f}^{2}}}{\Delta f}=\frac{\sum_{j=1}^{10} \overline{i_{f j}^{2}}}{g_{m 1}^{2} \Delta f}=\frac{2\left(\overline{i_{f 1}^{2}}+\overline{i_{f 3}^{2}}+\overline{i_{f 5}^{2}}+\overline{i_{f 7}^{2}}+\overline{i_{f 9}^{2}}\right)}{g_{m 1}^{2} \Delta f} \tag{4.8}
\end{equation*}
$$

In the similar way as for the thermal noise, the spectral density of the input referred flicker noise can be derived and is given by

$$
\begin{equation*}
\frac{\overline{v_{f}^{2}}}{\Delta f}=\frac{2 K_{f p}}{g_{m 1}^{2} f C_{o x} W_{1} L_{1}}\left[I_{D S 1}^{A_{f p}}+W_{1} L_{1}\left(\frac{K_{f n} I_{D S 3}^{A_{f n}}}{K_{f p} W_{3} L_{3}}+\frac{K_{f n} I_{D S 5}^{A_{f n}}}{K_{f p} W_{5} L_{5}}+\frac{I_{D S 7}^{A_{f p}}}{W_{7} L_{7}}+\frac{I_{D S 9}^{A_{f p}}}{W_{9} L_{9}}\right)\right] \tag{4.9}
\end{equation*}
$$

The total spectral noise density in the operational amplifier is the sum of the spectral density of the thermal and flicker noise

$$
\begin{equation*}
S_{o p}(f)=\frac{\overline{v^{2}}}{\Delta f}=\frac{\overline{v_{t h}^{2}}+\overline{v_{f}^{2}}}{\Delta f} . \tag{4.10}
\end{equation*}
$$

The $W / L$ transistor ratios are given in Figure 4.1 while the drain-to-source currents and transconductances for $M_{1}$ through $M_{10}$ are listed in Table 4.1. Also, noise parameters such as flicker noise coefficients and exponents of the PMOS and NMOS transistors in AMS $0.8 \mu \mathrm{~m}$ CMOS technology are listed in Table A. 1 of Appendix A. For the folded cascode operational amplifier the spectral noise densities of the thermal and flicker noise at 100 kHz have been calculated from (4.7) and (4.9) and their values are $32 \mathrm{nV} / \sqrt{\mathrm{Hz}}$ and $5 \mathrm{nV} / \sqrt{\mathrm{Hz}}$, respectively. Therefore the total spectral noise density in the operational amplifier calculated from (4.10) is $33 \mathrm{nV} / \sqrt{\mathrm{Hz}}$. The noise in the operational amplifier has been also determined after simulations with SPICE. The simulation and calculation values of the noise agree well and are given in Table 4.3.

### 4.5 Summary

In this chapter the folded cascode amplifier has been examined and its gain, bandwidth, and noise performance have been characterised. One of the advantage of the folded cascode amplifier is that its frequency response is dominated by the pole associated with its load capacitance. Therefore no internal compensation is needed to ensure stability. The amplifier is used in the analog memory architecture introduced in Chapter 3. The amplifier provides sufficient gain, bandwidth, and low noise compared with the noise of the analog memory.

The amplifier operates from a single +5 V power supply with a power dissipation of $653 \mu \mathrm{~W}$. The bias circuitry that generates the reference voltages for the amplifier was included on the chips. The amplifier characteristics were simulated in both voltage follower and inverter configurations. The simulations predict an open-loop gain of 98 dB , a phase margin of 90 degree, a unity-gain bandwidth of 1.92 MHz , and a -3 dB bandwidth of 25 Hz with a 10 pF load capacitance.

## Chapter 5

## Control Circuits

### 5.1 Overview

The control circuits are necessary to provide the write and read addresses for the analog memory core. The write and read control circuits are included on-chip and described in detail in this chapter. The write control circuit was implemented to achieve 500 MHz sampling frequency and its architecture is presented in Section 5.2. The following section describes the read control circuits which operate at 100 kHz readout frequency. The write control circuit is identical for both chips while the read control circuit is different. The performance of the control circuits is also evaluated.

### 5.2 High Speed Addressing Circuit

### 5.2.1 Circuit Description

Generally, shift registers are used for write address control in analog memory circuits. At sampling rates above 150 MHz (depending of the technology) this approach is difficult to implement and therefore delay chains are used instead. Such inverter chains have been employed previously in digital applications. The high speed write control circuit proposed for the analog memory consists of four 32 cell delay chains [27, 28]. An inverter delay chain of 32 cells together with a servo feedback illustrated in Figure 5.1 were implemented to reach 500 MHz sampling frequency. Each delay element in the chain consists of five MOS transistors, as indicated by the shaded box in Figure 5.1. A write pulse applied at input $\operatorname{In} 1$ propagates through the delay elements, producing the write address signals $w<1>$ through $w<32>$ for the analog memory core. The minimum width of the write pulse In 1 is constrained by the accuracy with which the analog signal is to be acquired and the input time constant of the sampling cell. The delay of the write pulse through the chain is set by the control voltage $\operatorname{Vctr} 1$ which determines the on resistance of the PMOS transistor $M_{1}$. The resistance together with the gate capacitance of the following inverter stage, $M_{4}$ and $M_{5}$, provide an adjustable $R C$ time delay that governs the sampling frequency of the memory.


Figure 5.1: Inverter delay chain of 32 cells and servo feedback circuit.

Shown in Figure 5.2 is a timing diagram of the write signals in one delay chain. In this mode several memory cells are addressed simultaneously. It should be noted that only the timing of the falling write clock edges is controlled by the circuit shown in Figure 5.1.

In order to ensure a delay, and thus the sampling frequency, a servo feedback circuit, also shown in Figure 5.1, is used. The raising edge of a reference input signal Aref1 is compared to the falling edge of the last write signal $w<32>$. When the delay is less than the intended value, as shown in Figure 5.3(a), the transistor $M_{6}$ turns on, which connects the current generated by $M_{8}-M_{9}$ mirror current to the capacitor $C_{1}$. The voltage across $C_{1}$ is increased, thereby slowing the inverter chain via the control voltage Vctr 1 . The signal Phi1 is included in such a way that the voltage across $C_{1}$ is modified only while the delays are being compared during the write phase. In the same way, as illustrated in Figure 5.3(b), when the delay is larger than the intended value, the voltage across $C_{1}$ is decreased. The time difference $t_{r e f}-t_{i n}$ determines the resulting write sample frequency, $f_{s}=32 /\left(t_{r e f}-t_{i n}\right)$. This feedback circuit eliminates the sensitivity of the delay chain to process parameters and compensates for the effect of temperature and supply variations.

The dimensions of the transistors in the delay chain and servo feedback circuit are indicated in Figure 5.1 in microns. The control logic which enables the transistors $M_{6}$ and $M_{7}$ was implemented with digital gates provided by the standard digital gates


Figure 5.2: Timing diagram of the write signals in one delay chain.


Figure 5.3: Timing diagram of the inverter chain showing the falling edge of the last write signal $w<32>$ which can be (a) before or (b) after the raising edge of the reference pulse Aref1.
library [39] of AMS $0.8 \mu \mathrm{~m}$ CMOS technology. The magnitudes of the currents for the two mirrors $M_{8}-M_{9}$ and $M_{10}-M_{11}$ are set by external resistors through $R 1 \mathrm{gnd}$ and $R 1 v d d a$. The size of the resistors determines the speed of charge or discharge of the capacitor $C_{1}$ during the write phase.

This dynamic servo feedback delay circuit can be used only for synchronous repetitive signal acquisition. Otherwise, the discharge of $C_{1}$ by leakage currents will introduce timing errors.


Figure 5.4: Timing errors after simulations in one delay chain.

### 5.2.2 Timing Accuracy

The timing accuracy within a signal channel is affected by delay variations among cells. The deviations from the nominal delay arise from inaccuracies in the fabrication process and are thus constant over time. The individual delay values shown in Figure 5.4 have been determined after simulations with SPICE [43]-[46] by applying a sine waveform to the input of the signal channel and fitting the output response to an ideal sine curve. It results a rms value of 160 ps for the element delay variation across 32 cells. This jitter corresponds to a sampling frequency error of $8 \%$ at the 500 MHz sampling rate. It should be noted that the jitter is independent of the input signal level and can be corrected for if required.

The total delay of the inverter chain is regulated by the feedback control circuit. Inaccuracies in this circuit manifest themselves as variations of the control voltage level $V \operatorname{ctr} 1$, and thus in a variation in the delay of the entire inverter chain. As a consequence, the sampling frequency may vary from one measurement cycle to the next.

It should be again noted that in the proposed analog memory design the turn off time of the sampling switches is independent of the input signal level, eliminating a timing error that would otherwise be present for high frequency input signals.

### 5.3 Read Addressing Circuits

### 5.3.1 Read Control Circuit for FASTSAMP-EV chip

The read control circuit for FASTSAMP-EV chip consists of four 32 stage dynamic twophase shift registers. Figure 5.5 illustrates one of the 32 stage dynamic two-phase shift register [26] configurations with the timing diagram. In this figure, Phis1 and Phis2 are the two non-overlapping clocks controlling the shift register, and Phirin1 is the serial input to the register. The schematic of the two-phase clock generator which provides the non-overlapping clocks is shown in Figure 5.6. The non-overlapping characteristic of the


Figure 5.5: A 32 stage dynamic two-phase shift register with timing diagram.


Figure 5.6: Two-phase clock generator.
resulting shift register clocks, Phis1 and Phis2, is ensured by the delays of the extra inverters. The signals $r<1>$ through $r<32>$ are the read address control signals for the analog memory core. The enable signal Phien 1 is used to disable the read addresses, $r<1>$ through $r<32>$, while the analog memory is reset between readout of two successive memory cells, as shown in Figure 3.4(b).

The shift register is initialised by raising both of the clocks, Phis1 and Phis2, and the serial input Phirin1 low, as shown in Figure 5.5. This sets the read address signals $r<1>$ through $r<32>$ to their low state. The shift register proceeds as follows. The serial input Phirin1 is set to high, and with a raising edge of clock Phis1, the first read address $r<1>$ becomes high. After clock Phis1 is returned to low, a Phis2 pulse advances the logic level of Phirin1 to the second inverter in the register. The serial input Phirin1 is then raised to the low state and, after another Phis1 pulse, the first address signal, $r<1>$, goes low, while the second address signal, $r<2>$, goes high. Consecutive clock pairs, Phis1 and Phis2, advance the logic levels within the shift register until the last read address control signal, $r<32>$, rises and falls, as illustrated in Figure 5.5. It is important to note that the shortest period of the non-overlapping shift register clocks must stay high is determined by the time required to adequately charge or discharge the inverter input gate capacitances through the pass transmission gates. The minimum time between two successive write clocks is therefore simply the sum of two inverter delays plus the timing overhead required to ensure that the shift registers clocks are non-overlapping.

The transistor dimensions for the transmission gates used as switches in Figure 5.5 are given in microns. To calculate the drawn dimensions of the PMOS and NMOS transistors, the relations (2.43) and (2.44) were used. Also, the inverters and the gates are provided by the standard digital gates library in AMS $0.8 \mu \mathrm{~m}$ CMOS technology.

### 5.3.2 Read Control Circuit for FASTSAMP-V1 chip

The readout of the FASTSAMP-V1 chip is controlled by an on-chip 1 of 128 decoder [28] shown in Figure 5.7. The decision to replace the four 32 stage dynamic two-phase shift registers by a 1 of 128 decoder was taken to approach more to the camera electronics requirements of the Cherenkov telescope. The schematic of the read control circuit consists of 1 of 4 decoders and 1 of 8 decoders. Both types of decoders with the schematics represented in Figure 5.8 were implemented with digital gates using the standard digital gates library of AMS $0.8 \mu \mathrm{~m}$ CMOS technology. A microcontroller which exists in the


Address6...Address0 $\times 1$
-• 127


Figure 5.7: Read control circuitry with timing diagram.
(a)

(b)


Figure 5.8: Schematics of the (a) 1 of 4 decoder and (b) 1 of 8 decoder.
camera electronics design of the Cherenkov telescope [1] provides 7 bit address signals Address0 through Address6, as illustrated in Figure 5.7. The signal Phien activates the decoders and thus enables the read signals $r<1>$ through $r<128>$. For the Cherenkov application is necessary to read out only a few samples depending of the analog input waveform. This decision is given by the microcontroller which provides the start and stop addresses through the address signals Address 0 to Address6.

### 5.4 Summary

Commonly shift registers are used for write addressing in an analog memory. At high sampling speeds, the variations in cell-to-cell sampling times due to the sensitivity of onchip delays are considerable, and extensive ac timing correction procedures are required. In addition, a high speed sampling clock must be provided to the circuit. This chapter proposed the use of inverter delay chains for write control circuit, which avoid the need for a high speed external clock. This write control circuit is insensitive to variations in the fabrication process, temperature and supply levels because servo feedback circuits are used to adjust the sampling rate. The sampling clock period is derived by a division of time delay between two external control signal edges by the number of sampling cells in one delay chain. The variations in cell-to-cell sampling times were estimated to be after simulations 160 ps rms which corresponds to a sampling frequency error of $8 \%$ at the 500 MHz sampling rate. This jitter is independent of the input signal level and can be corrected.

The read control circuit was implemented with dynamic two-phase shift registers or with a 1 of 128 decoder depending of the chip version.

## Chapter 6

## Memory Calibration and Correction Procedures

### 6.1 Introduction

It is essential to have in analog memory an uniform response in a large number of memory cells according with the accuracy of the technology. The parameters which characterise an analog memory are cell-to-cell offset and gain variations within a memory channel. In high precision applications the cell non-uniformities may not be adequate and must therefore be cancelled by correcting the data. Dc correction procedures and ac calibration [26] may be required if the memory does not satisfy the performance objectives. The calibration and correction procedures are needed to eliminate variations of the cell offsets, gains and nonlinearities. In large systems is necessary to reduce the computational effort and the number of components required to store the correction constants.

The voltage $V_{o i}$ read out from a given memory cell $i$ can be expressed as a function of the input voltage $V_{i n}$,

$$
\begin{equation*}
V_{o i}=H_{i} V_{i n} \tag{6.1}
\end{equation*}
$$

where $H_{i}$ is referred to as the transfer function of memory cell $i$. Ideally, the transfer function of all cells are identical and equal to one but in reality will not because of gain, nonlinearity, and offset variations among cells. The origin of these variations can be inaccuracies in the fabrication process and control signal feedthrough while the circuit is being operated.

In large systems is necessary to reduce the computational effort and the number of components required to store the correction constants. The calibration is performed by applying known sets of signals at the analog input and storing the resulting output values. The transfer function $H_{i}$ is then calculated, and the inverse function of $H_{i}$ is used to correct the acquired data. The cell correction values are expressed in the form of calibration constants. The time needed to determine these constants during the calibration procedure is generally not crucial and the correction can be done on-line. The goal is to minimise the number of calibration constants and the time required to correct the signal data.


Figure 6.1: Dc correction procedure using a subtraction method.

### 6.2 DC Calibration

Three dc correction procedures such as subtraction, multiplication and addition, and piece-wise linear approximation are presented in the following subsections. Each procedure is described in detail.

### 6.2.1 Subtraction Method

A subtraction procedure can be implemented with a digital circuit as illustrated in Figure 6.1. The correction steps for cell $i$ are the following.

During calibration, the reference calibration voltage $V_{c a l}$ is applied at the input and the digitised output voltage levels are transferred into the digital memory. The known reference voltage $V_{c a l}$ is identical for the entire acquisition system. The corresponding output voltage of cell $i, V_{o c i}$, is

$$
\begin{equation*}
V_{o c i}=V_{c a l}+V_{o f f i}=K_{i}, \tag{6.2}
\end{equation*}
$$

where $V_{o f f i}$ is the memory cell offset voltage and $K_{i}$ is the calibration constant to be stored for cell $i$.

During data acquisition, the input signal voltage $V_{s i g}$ is applied and the corresponding output voltage $V_{o i}$ of cell $i$ is

$$
\begin{equation*}
V_{o i}=V_{s i g}+V_{o f f i} . \tag{6.3}
\end{equation*}
$$



Figure 6.2: Dc correction procedure using a multiplication and addition method.

The input voltage $V_{\text {sig }}$ can be determined by subtracting ( $K_{i}-V_{\text {cal }}$ ) from the output response $V_{o i}$,

$$
\begin{equation*}
V_{s i g}=V_{o i}-V_{o f f i}=V_{o i}-\left(K_{i}-V_{c a l}\right) . \tag{6.4}
\end{equation*}
$$

The subtraction is done by a digital subtracter in Figure 6.1.
If the analog memory has $N$ cells then $N$ constants need to be stored. It should be noted that the subtraction method corrects the offset voltage errors for dc input signals.

### 6.2.2 Multiplication and Addition Method

The multiplication and addition method requires two reference voltages, as illustrated in Figure 6.2. The circuit response to the reference voltages is

$$
\begin{equation*}
V_{o c i 1}=A_{i} V_{c a l 1}+V_{o f f i} \tag{6.5}
\end{equation*}
$$

and

$$
\begin{equation*}
V_{o c i 2}=A_{i} V_{c a l 2}+V_{o f f i}, \tag{6.6}
\end{equation*}
$$

where $A_{i}$ is the voltage gain of cell $i, V_{o c i 1}$ and $V_{o c i 2}$ are the responses of the circuit to reference voltages $V_{c a l 1}$ and $V_{c a l 2}$, respectively. When the input voltage $V_{s i g}$ is applied, the corresponding output voltage $V_{o i}$ is

$$
\begin{equation*}
V_{o i}=A_{i} V_{s i g}+V_{o f f i} . \tag{6.7}
\end{equation*}
$$

Therefore the input voltage $V_{\text {sig }}$ can be determined,

$$
\begin{equation*}
V_{s i g}=K_{1 i} V_{o i}+K_{2 i}, \tag{6.8}
\end{equation*}
$$



Figure 6.3: Dc correction procedure using a piece-wise linear approximation method.
where $K_{1 i}$ and $K_{2 i}$ are two calibration constants for each cell. These calibration constants are derived from (6.5) through (6.7) and written as follows

$$
\begin{gather*}
K_{1 i}=\frac{1}{A_{i}}=\frac{V_{c a l 2}-V_{c a l 1}}{V_{o c i 2}-V_{o c i 1}}  \tag{6.9}\\
K_{2 i}=-\frac{V_{o f f i}}{A_{i}}=V_{c a l 1}-K_{1 i} V_{o c i 1} . \tag{6.10}
\end{gather*}
$$

An analog memory channel with $N$ cells requires $2 N$ constants need to be stored. The number of constants required can be reduced when the gain matching among cells is satisfactory. The input signal $V_{\text {sig }}$ can be expressed

$$
\begin{equation*}
V_{s i g}=K_{1} V_{o i}+K_{2 i} \tag{6.11}
\end{equation*}
$$

and only $(N+1)$ constants need to be stored. The multiplication and addition method corrects both cell-to-cell gain and offset voltage errors for dc input signals.

### 6.2.3 Piece-Wise Linear Approximation Method

The nonlinearities in the circuit response can be corrected using a piece-wise linear approximation method. The number of calibration voltage levels is determined by the number

| Non-Ideal <br> Parameter | Correction <br> Procedure | Number of <br> Calibration <br> Voltage Levels | Number of <br> Constants per <br> Memory Cell |
| :--- | :--- | :--- | :--- |
| Offset | Subtraction | 1 | 1 |
| Gain and <br> Offset | Multiplication and <br> Addition | 2 | 2 |
| Linearity | Piece-Wise Linear <br> Approximation | Number of <br> Segments +1 | $2 \times$ Number of <br> Segments |

Table 6.1: Calibration and correction parameters.
of linear segments needed to obtain the desired accuracy, as shown in Figure 6.3. In this figure a nonlinear transfer curve is approximated by four linear segments. The five calibration voltages are $V_{c a l 1}$ through $V_{c a l 5}$, and the corresponding memory responses are $V_{o c i 1}$ through $V_{o c i 5}$. During data acquisition, the input signal voltage $V_{\text {sig }}$ can be approximated from the measured output voltage $V_{o i}$ by a linear interpolation between the nearest calibration output values.

The procedures listed in Table 6.1 are sufficient to cancel cell offset, gain and nonlinearity errors for dc input signals. In table are listed the operations that must be performed to correct offset, gain, and linearity errors, with the number of reference voltage levels and constants needed for these operations.

### 6.3 AC Calibration

A variation in the sampling time interval from cell to cell generates an amplitude error, as is illustrated in Figure 6.4. In this example, a ramp input signal is sampled at four distinct times, $t_{1}$ through $t_{4}$, on the falling edges of write signals $w<1>$ through $w<4>$ and stored in four consecutive analog memory cells. The time $t_{2}^{\prime}$ is the nominal sample time and $t_{2}$ is the actual sample time when the second sample is stored. A deviation $\Delta t_{2}=t_{2}-t_{2}^{\prime}$ results in an amplitude error

$$
\begin{equation*}
\Delta V_{o 2}=\frac{d V_{i n}}{d t} \Delta t_{2} \tag{6.12}
\end{equation*}
$$

where $d V_{i n} / d t$ is the slope of the input voltage signal. Typical values for deviations $\Delta t_{i}$ in one delay chain of 32 cells are shown in Figure 5.4.

It should be noted that the time deviations $\Delta t_{i}$ are stable and independent of the input signal level. The sample time $t_{i}$ associated with a given memory cell location $i$ is simply adjusted by a correction factor $\Delta t_{i}$ that is obtained from a single ac input waveform during calibration. These correction factors can be determined from a ramp or sine wave input signal and are applicable to all input signal shapes and frequencies.

The high frequency input signals generate timing errors, as was investigated in Chapter 2. Complex ac calibration and dc correction procedures may be required if the memory does not satisfy the performance objectives.


Figure 6.4: Effect of sample time error on the reconstructed output of four write signals showing the actual sample time of the write signal $w<2>$ which can be (a) after or (b) before the nominal sample time.


Figure 6.5: Input signal as (a) ramp wave or (b) signal from Cherenkov telescope.

### 6.4 Method to Calibrate Signals from Cherenkov Telescopes

The signals provided by Cherenkov telescopes are short pulses and is necessary mixed calibration (dc and ac calibration). The correction steps for cell $i$ are the following:

- A dc calibration using multiplication and addition method or piece-wise linear approximation method should be performed.
- After dc calibration, a ramp wave input signal is applied, as illustrated in Figure 6.5(a). The slope $d V_{\text {sig }} / d t$, the nominal sample time $t_{i}^{\prime}$, and the amplitude error $\Delta V_{o i}$ can be easily determined. It is known that

$$
\begin{equation*}
\Delta t_{i}=t_{i}-t_{i}^{\prime} \tag{6.13}
\end{equation*}
$$

and

$$
\begin{equation*}
\Delta V_{o i}=\frac{d V_{s i g}}{d t} \Delta t_{i} \tag{6.14}
\end{equation*}
$$

Therefore the actual sample time $t_{i}$ can be calculated from (6.13) and (6.14)

$$
\begin{equation*}
t_{i}=t_{i}^{\prime}+\frac{\Delta V_{o i}}{\frac{d V_{s i g}}{d t}} \tag{6.15}
\end{equation*}
$$

- At the input of the analog memory is applied a Cherenkov pulse. The signal must be reconstructed on $t_{i}$, as illustrated in Figure 6.5(b).


### 6.5 Summary

The challenge in analog memory design is to produce an uniform and linear response in a large number of memory cells. Principal issues are cell-to-cell offset and gain variations within a memory channel, which are governed by the circuit architecture and its sensitivity to the matching properties of its constituent components.

The performance of an analog memory and the desired accuracy determine the complexity of the inverse function of $H_{i}$, and therefore the number of calibration voltage levels to be applied during calibration. The cancellation of memory cell offset voltages requires a subtraction procedure with one calibration constant for each cell. The multiplication and addition method corrects both cell-to-cell gain and offset voltage errors and requires two reference voltages while the nonlinearities are corrected by piece-wise linear approximation method. Complex ac calibration and data correction procedures are required to calibrate signals from Cherenkov telescopes.

## Chapter 7

## Simulation and Experimental Results

### 7.1 Overview

In this chapter the simulation and experimental results for two devices are presented. Section 7.2 describes the layouts of the chips together with some design optimisations. The results after ideal and parasitic simulations with a common simulation setup are reported in Section 7.3. The noise performance of the analog memories is limited by the noise in amplifiers, as will be shown in Section 7.4. The test setups used to measure the performance of the experimental circuits are described in Appendix C and Appendix D, and the results from these measurements are reported in Section 7.5. The output responses of the two versions to dc inputs are different. A significant improvement in dc response has been reached for FASTSAMP-V1 device compared with FASTSAMP-EV device.

### 7.2 Chips Layout

Two chips FASTSAMP-EV and FASTSAMP-V1 were designed [47, 48] at the Heidelberg ASIC laboratory in the Austria Microsystems (AMS) $0.8 \mu \mathrm{~m}$ CMOS technology [41] with poly-to-poly capacitors. The prototypes were produced by Nordic VLSI ASA company in Norway. The first chip designed was FASTSAMP-EV followed by FASTSAMP-V1. Figure 7.1 and Figure 7.2 show the layout views of the FASTSAMPEV and FASTSAMP-V1, respectively. The layouts measure $3.26 \mathrm{~mm} \times 3.37 \mathrm{~mm}$ and $3.26 \mathrm{~mm} \times 3.39 \mathrm{~mm}$, respectively. The layouts of the chips are approximatively the same with minor changes. The reason is that the write control circuit and the analog memory core are identically for both chips while the read control circuit is different. The circuits have been carefully laid out to minimise the parasitic capacitances and coupling between the control and signal traces. The large input transistors are seen on the left and the amplifiers appear on the right of the analog memory channels. The feedback delay control circuits are located near to the operational amplifiers. The power supply is uniform distributed and separated into analog (Analog1vdda through Analog4vdda) and digital (Digital1vdd through Digital4vdd). The corresponding grounds are identified by Analog1gnd through Analog4gnd and Digital1gnd through


Figure 7.1: Layout view ( $3.26 \mathrm{~mm} \times 3.37 \mathrm{~mm}$ ) of the FASTSAMP-EV chip.


Figure 7.2: Layout view ( $3.26 \mathrm{~mm} \times 3.39 \mathrm{~mm}$ ) of the FASTSAMP-V1 chip.


Figure 7.3: Schematic (upper) and layout (lower) of an analog memory cell.


Figure 7.4: Response after simulations of one channel to a 2 V peak-to-peak, 3.906250 MHz sine wave sampled at 500 MHz . The pulse is plotted on the (a) read and the (b) write time scale.

Digital4gnd, respectively. The delay chains, feedback delay control circuits, amplifiers are connected to the analog power supply while the switches and read control circuits to the digital power supply. All analog and digital pads are protected electrostatically to avoid discharge and destruction of the chips. Ringvdd and Ringgnd are the power supply connections to all digital and analog pads around the chips.

The layout of each chip is divided on four blocks of 32 cells. Each block consists of an inverter delay chain, an analog memory and a read control circuit. One block of 32 cells is connected to an analog power supply Analogkvdda and to a digital power supply Digitalk $v d d$, where $1 \leq k \leq 4$.

The schematic and layout of an analog memory cell are shown in Figure 7.3. As was mentioned in Chapter 3, an analog memory cell consists of a write transistor $M_{w i}$, a read transistor $M_{r i}$, and a sampling capacitor $C_{i}$. The layout area occupied by one analog memory cell is $37 \mu \mathrm{~m} \times 66 \mu \mathrm{~m}$. Since the AMS $0.8 \mu \mathrm{~m}$ CMOS process provides two polysilicon layers (poly 1 and poly 2), the storage capacitor $C_{i}$ is implemented as a poly-to-poly capacitance. The capacitance is surrounded by a guard ring connected to the analog ground. Two metal layers (metal 1 and metal 2) were used for routing. Connections to the input bus, read bus, analog ground and $V_{C}$ are done with metal 1 while for $w<i>$ and $r<i>$ with metal 2. The $M_{w i}$ and $M_{r i}$ transistors can be


Figure 7.5: Response after simulations of one analog memory cell to a 2 V peak-to-peak, 3.906250 MHz sine wave sampled at 500 MHz after (a) ideal and (b) parasitic simulations. The pulse is plotted on the read time scale.
recognised in the layout by the intersection of diffusion and poly 1 layer representing the gate area. Contacts connect diffusion or polysilicon with the routing layer metal 1 , whereas metal 1 and metal 2 are connected by vias. This layout configuration of an analog memory cell minimises the parasitic capacitance of the input bus.

### 7.3 Simulation Results

FASTSAMP-EV and FASTSAMP-V1 were simulated with SPICE [43]-[46]. Ideal and parasitic simulations were performed and the simulation setup was identically for both chips. The response after ideal simulations of one channel to a 2 V peak-to-peak (from 1.5 V up to 3.5 V ) input sine waveform is shown in Figure 7.4(a) and illustrates the operation of the circuit with $V_{C}$ and $V_{B}$ set to 2.5 V . The output signal levels of the 128 memory cells are alternated with the amplifier reset level, $V_{B}$, as illustrated in the timing diagram in Figure 3.4(b). The readout time for each cell was set to $10 \mu \mathrm{~s}$ and reset time to $1 \mu \mathrm{~s}$. In Figure $7.4(\mathrm{~b})$ the output pulse is plotted as a function of input time, and the results agree with the input pulse. The input signal range of 2 V has been chosen according with (3.14) and (3.15) to avoid the subthreshold leakage.

The parasitic simulations included all parasitic capacitances extracted from layouts. The results after ideal and parasitic simulations for one memory cell are shown in Figure 7.5 (a) and (b), respectively. It should be noted the effect of the parasitic capacitances on the raising edge of the pulse represented in Figure 7.5(b).

Both ideal and parasitic simulations were performed without using load capacitances at the outputs of the operational amplifiers. As was discussed in Section 4.3, 10 pF load capacitances must be considered for real applications.
(a)
(b)


Figure 7.6: Circuit for analysis of analog memory noise during the (a) write and (b) read phase.

### 7.4 Analog Memory Noise

The output voltage of the analog memory circuit is contaminated by noise. The main sources of noise are thermal and flicker noise generated in the switches and in the operational amplifiers, and noise coupled directly or capacitively through the power, ground, clock lines, and through the substrate. The power supply lines must be bypassed to ground sufficiently to attenuate potential noise sources. Noise injected from clock lines into circuit nodes and into the substrate may contribute to the pedestal voltage of a memory cell.

In order to investigate the noise performance of the analog memories, the simplified circuits shown in Figure 7.6 are considered, which correspond to the write and read configuration, respectively. $C_{o p}$ is the parasitic capacitance at the inverting amplifier input and is dominated by the capacitance of the read bus to ground $C_{r d b}$. The value of $C_{r d b}$ has been extracted from the layout of the analog memory core and listed in Table A. 2 of Appendix A. In the write phase when the write switch is turned off the thermal noise voltage is given by $k T / C_{i}[31]$, where $k=1.38 \times 10^{-23}[\mathrm{~J} / \mathrm{K}]$ is the Boltzmann's constant and $T$ is the absolute temperature. During the read phase the capacitor $C_{i}$ is switched across the amplifier, and the square of the total noise voltage for the analog memory is given by

$$
\begin{equation*}
\overline{v_{n}^{2}}=\frac{k T}{C_{i}}+\left(\frac{C_{i}+C_{o p}}{C_{i}}\right)^{2} \overline{v_{o p}^{2}} \tag{7.1}
\end{equation*}
$$

where $\overline{v_{o p}^{2}}$ is the input referred noise from the amplifier. In order to obtain the amplifier noise voltage, $\overline{v_{o p}^{2}}$, the amplifier noise power density $S_{o p}(f)$ in (4.10) must be multiplied by a noise transfer function and integrated over the unity-gain bandwidth $f_{u}(1.92 \mathrm{MHz})$ of the amplifier. Since the reset switch, $M_{\text {reset }}$, across the amplifier in Figure 7.6(b) is closed


Figure 7.7: Picture taken from the oscilloscope representing three channels Ch1: AnalogOutputCh1, Ch2: TriggerScope and Ch3: ComIn or ComInOut depending of the chip version.
and opened before the memory cell is addressed for readout, the circuit forms a correlated double sampling (CDS) system [32]. It is known that the noise transfer function of a CDS system is given by

$$
\begin{equation*}
H(f)=2 \sin \left(\frac{2 \pi f T_{s}}{2}\right) \tag{7.2}
\end{equation*}
$$

where $T_{s}$ is the interval from the time when the reset switch is turned off until the time when the analog memory cell is addressed for readout. The time interval $T_{s}$ was $9 \mu \mathrm{~s}$ during measurements. The noise contributed from the amplifier in Figure 7.6(b) is given by

$$
\begin{equation*}
\overline{v_{o p}^{2}}=\int_{0}^{f_{u}} S_{o p}(f) H^{2}(f) d f \tag{7.3}
\end{equation*}
$$

The total circuit noise in the system, expressed by (7.1), is theoretically

$$
\begin{equation*}
\overline{v_{n}}=\sqrt{\left(8280 \mu V^{2}\right)+(7.6)^{2}\left(3974 \mu V^{2}\right)}=488 \mu V \tag{7.4}
\end{equation*}
$$

It is therefore concluded that the total circuit noise is limited by the noise in the amplifier.

| Device Name |  |  | FASTSAMP-EV | FASTSAMP-V1 |
| :---: | :---: | :---: | :---: | :---: |
| Parameter | Symbol | Calculation | Measurement | Measurement |
| Cell gain | $A_{i}$ | 0.979 | 0.982 | 0.972 |
| Cell offset voltage | $V_{\text {offi }}$ | 141 mV | 147 mV | 136 mV |

Table 7.1: Calculation and measurement results for both devices.

### 7.5 Experimental Results

The experimental test setups used to evaluate the performance of the analog memory circuits are described in detail in Appendix C and Appendix D. The dc and ac results presented in this section are thus representative for the performance of both devices. The dc power dissipations for FASTSAMP-EV and FASTSAMP-V1, when operated from +5 V analog and +5 V digital supplies, were measured to be 50 mW and 35 mW , respectively, and were dominated by dissipation of the output amplifiers, delay chains and servo feedback circuits.

In order to measure the dc or ac voltages stored in analog memory cells in one analog memory channel a signal TriggerScope was created, as illustrated in Figure 7.7. Depending of the chip version, the signal ComIn or ComInOut was applied to the third channel of the oscilloscope as a trigger signal. The waveforms were transfered via GPIB [52] interface from the oscilloscope to a Hewlett Packard workstation. At each edge of signal TriggerScope a dc or ac voltage stored in a memory cell is read out. This was possible by programming in C and $\mathrm{C}++$ programming languages $[35,36]$.

The dc and ac measurements for FASTSAMP-EV device were performed for 128 cells in one channel. Unfortunately for FASTSAMP-V1 device was only possible to perform measurements over 32 cells (instead of 128 cells), because the rest of the cells were not working properly. After investigation of this problem it was assumed that its cause is a technology failure. Due to limitation in time a new submission in fabrication was not possible.

### 7.5.1 DC Transfer Characteristic

The input voltage range of 1.5 V (from 2 V up to 3.5 V ) has been chosen for measurements according with the nonlinearities of the output amplifiers and with (3.14) and (3.15) to avoid the subthreshold leakage. This input signal range was set for both devices.

The measured pedestal voltages uncorrected for the 32 cells of FASTSAMP-V1 device are plotted in Figure 7.9 as a function of the input voltage. The cell-to-cell pedestal variations result in a deviation from the average of 50 mV . This deviation is determined by the control signal feedthrough on-chip and on printed circuit board (PCB) and by the fabrication process used. The deviation for the 128 cells in one channel of FASTSAMP-EV device was of 150 mV . This improvement of the deviation in FASTSAMP-V1 device was determined through a carefully layout of the PCB. The cell-to-cell pedestal variations are not accepted for the Cherenkov application and therefore dc and ac calibrations must be performed. As dc calibration the multiplication and addition method with two calibration


Figure 7.8: Cell pedestals after calibration as a function of input voltage for the 128 memory cells. Dc measurements for FASTSAMP-EV device.
voltages ( $V_{\text {cal } 1}=2 \mathrm{~V}$ and $V_{\text {cal2 }}=3.5 \mathrm{~V}$ ) was used to correct both cell-to-cell gain and offset voltage errors for dc input signals.

In order to investigate whether the cell pedestals depend on the input signal, the responses to various dc input levels were recorded, and the responses after dc calibration using a multiplication and addition method are plotted in Figure 7.8 and Figure 7.10, respectively, as a function of the input voltage. The rms cell response variation across the full input range is 10 mV for both devices, demonstrating that the sampling switch charge injection is independent of the dc input level and can be reduced by a simple calibration procedure.

The cell gain and offset voltage variations for devices are plotted as a function of cell number, as illustrated in Figure 7.11 and Figure 7.12, respectively. The average gains were measured to be 0.982 and 0.972 , with an rms gain variation of 0.01 , as indicated by Figure 7.11 and Figure 7.12. The average offsets were measured to be 147 mV and 136 mV , respectively. The values calculated for gain $A_{i}$ and offset $V_{o f f i}$ from (3.12) and (3.13) approximately agree with the measured values, as listed in Table 7.1.

The nonlinearity of each device was measured by applying 31 equally spaced input voltages and plotting the output levels as a function of input levels. Figure 7.13 and Figure 7.14 show the output of a typical cell and the deviations plotted as a function of input voltage over a range of 1.5 V . The maximum deviation in each case is 20 mV , or $1.3 \%$


Figure 7.9: Cell pedestals before calibration as a function of input voltage for the 32 memory cells. Dc measurements for FASTSAMP-V1 device.


Figure 7.10: Cell pedestals after calibration as a function of input voltage for the 32 memory cells. Dc measurements for FASTSAMP-V1 device.


Figure 7.11: Cell gain (upper) and cell offset voltage (lower) as a function of cell number for FASTSAMP-EV device.


Figure 7.12: Cell gain (upper) and cell offset voltage (lower) as a function of cell number for FASTSAMP-V1 device.


Figure 7.13: Upper: Output plotted as a function of input voltage. Lower: Deviations for the selected 1.5 V input signal range. Dc measurements for FASTSAMP-EV device.


Figure 7.14: Upper: Output plotted as a function of input voltage. Lower: Deviations for the selected 1.5 V input signal range. Dc measurements for FASTSAMP-V1 device.
of the chosen input voltage range of 1.5 V .

### 7.5.2 Dynamic Range

The dynamic range of an analog memory circuit [26] is commonly defined as the maximum recordable signal divided by the baseline noise. The baseline noise of these analog memories was determined by recording the response of the devices to repeated measurements $[33,34]$ with a constant input voltage level and by calculating the mean square rms voltage error

$$
\begin{equation*}
\overline{v_{r m s}}=\frac{\sqrt{\sum_{i=1}^{M}\left(V_{o i}-V_{a v g}\right)^{2}}}{\sqrt{M-1}} \tag{7.5}
\end{equation*}
$$

where $V_{o i}$ is the output voltage of cell $i$ and $V_{\text {avg }}$ is the average of $M$ measurements,

$$
\begin{equation*}
V_{a v g}=\frac{1}{M} \sum_{i=1}^{M} V_{o i} . \tag{7.6}
\end{equation*}
$$

An rms error voltage of 10 mV for each device was obtained from sets of 100 repeated measurements. The dynamic range is therefore better than $150 / 1$, or 8 bits, for a 1.5 V input voltage range.

### 7.5.3 AC Response

Figure 7.15 shows the response of FASTSAMP-V1 device to a 1.5 V peak-to-peak gaussian pulse sampled at 500 MHz . At 3 V amplitude of the input signal the width of the gaussian pulse is 10 ns . On the reconstructed output signal can be seen five samples which corresponds to 10 ns , as illustrated in Figure 7.15(c). This proves that the sampling frequency is stable in time. It should be noted that the response of the device to a gaussian pulse is shown without using a calibration procedure.

The response of FASTSAMP-V1 device to a rectangle pulse with a 6 ns rise time is shown in Figure 7.16. In Figure 7.16(c) the output pulse is plotted as a function of input time, and the results agree with the input pulse, as monitored on an oscilloscope, with respect to rise time, fall time and pulse width.

The ac performances of the devices were evaluated applying sine waves at the analog inputs. The pedestal subtracted responses of 20 separate sets of measurements are shown in Figure 7.17 and Figure 7.18, respectively. The deviations of the measured data from the ideal sine waves are plotted and a rms error voltage of 10 mV was calculated for each device. The errors can be attributed to a variety of sources, including errors in sampling time, variations in the ac response of different cells, nonlinearities, and electronic noise.


Figure 7.15: Response after measurements of 32 cells to a 1.5 V peak-to-peak (a) gaussian pulse sampled at 500 MHz . The pulse is plotted on the (b) read and the (c) write time scale. Ac measurements for FASTSAMP-V1 device.


Figure 7.16: Response after measurements of 32 cells to a 1.5 V peak-to-peak (a) rectangle pulse sampled at 500 MHz . The pulse is plotted on the (b) read and the (c) write time scale. Ac measurements for FASTSAMP-V1 device.


Figure 7.17: Results of 20 measurement sets from a 1.5 V peak-to-peak, 3.906250 MHz sine wave sampled at 500 MHz . Residuals are plotted as a function of cell number for FASTSAMP-EV device.


Figure 7.18: Results of 20 measurement sets from a 1.5 V peak-to-peak, 15.625 MHz sine wave sampled at 500 MHz . Residuals are plotted as a function of cell number for FASTSAMP-V1 device.

| Device Name | FASTSAMP-EV | FASTSAMP-V1 |
| :--- | :---: | :---: |
| Cell pedestal variations across <br> full input range of 1.5 V <br> uncorrected <br> corrected |  |  |
| Nonlinearity (for 1.5 V full scale) | 150 mV |  |
| Cell gain non-uniformity | 10 mV | 50 mV |
| Dynamic range | $1.3 \%$ | 10 mV |
| Acquisition time | 8 bits | $1.3 \%$ |
| RMS timing error <br> in one delay chain | 1600 ps | $1 \%$ (mean gain: 0.972 ) |
| Sampling frequency | 500 MHz | 8500 ps |
| Readout frequency | 100 kHz | 160 ps |
| Power dissipation on <br> device <br> PCB | 50 mW | 500 MHz |

Table 7.2: Performances for both devices.

### 7.6 Summary

The implementation of two analog memory circuits have been described in this chapter. Two chip versions were fabricated; a first experimental chip FASTSAMP-EV followed by FASTSAMP-V1 which is more approached to the camera electronics. Measurement results at sampling rate of 500 MHz were presented. The dc and ac results of the performance tests are summarised in Table 7.2.

It was shown that the baseline noise that was measured for the fabricated analog memory circuits is limited by the noise in the amplifier. Theoretically, the value of the total noise calculated by (7.4) of $488 \mu \mathrm{~V}$ should agree with the rms error voltage of 10 mV from (7.5) after measurements. This difference between the two noise values may be due to perturbations caused by the power supply (e.g. ringing), ground, control signals, routed on board traces to the chip packages.

## Chapter 8

## Conclusions and Suggestions

### 8.1 Conclusions

Many acquisition systems require the recording of analog waveforms at a high rate and with high resolution. In applications such pulse echo phenomena (radar, ultrasonics), pulse shape recording (high energy physics experiments), and laboratory instrumentation (oscilloscopes, transient digitisers), the analog waveforms need only to be captured for a limited period of time and a continuous digitisation is not required.

This research has concentrated on switched capacitor analog memories. The goal of this research was to investigate analog memories for waveform sampling at several hundred MHz . An effort was devoted to optimise the analog memory architecture and circuit implementation for uniformity of memory cell responses within a channel. This is especially important in Cherenkov application, where analog waveforms of hundreds of channels are recorded. In this application it is also important to minimise the complexity of dc and ac calibration, as well as the number of calibration constants needed to correct the data.

After an examination of the characteristics of MOS switches and capacitors, this work has analysed their performance in a number of sample and hold configurations wherein the switch can be inserted in the signal or signal return paths. Expressions for the error voltages from switch charge injection and clock feedthrough effect were derived for circuits wherein the sampling capacitance is not large compared to the parasitic capacitances associated with the sampling switch. It was analytically shown that the sampling switch must be inserted in the signal return path to eliminate cell specific gain and sampling time errors that are dependent on the input signal level.

Based on the results from the investigation of the sample and hold circuits, an analog memory architecture was proposed. The transfer function of this memory was derived and then verified by measurement results obtained from two devices. It was shown that the memory cell pedestal voltages are independent of the input signal voltage and that the cell specific voltages can be cancelled by a simple multiplication and addition procedure.

Each channel of the analog memory incorporates an on-chip operational amplifier for readout. The amplifier provides sufficient gain, bandwidth, and low power dissipation.

The results from simulations and calculations show that the folded cascode amplifier circuit is well suited for use in this application.

At high sampling speeds, the variations in cell-to-cell sampling times due to the sensitivity of on-chip delays to the fabrication process, the temperature, and the power supply levels are considerable, and extensive dc and ac timing timing correction procedures are required. In addition, a high speed sampling clock must be provided to the circuit. This thesis proposed the use of inverter chains for write control, which avoid the need for a high speed external clock. This write control circuit is insensitive to variations in the fabrication process, temperature, and supply levels because servo feedback circuits are used to adjust the sampling rate. Furthermore, the high speed write signals are confined to a small area on the dies, and perturbations from external clocks that otherwise must be distributed across the chips are avoided.

Two 4 channel $\times 128$ cell analog memories for use in Cherenkov application were fabricated in a AMS $0.8 \mu \mathrm{~m}$ CMOS technology with poly-to-poly capacitors, and operated at sampling rate of 500 MHz . The cell-to-cell sampling time variation is 160 ps rms . The acquisition time of the analog memories for a given accuracy is less than 500 ps . The measured nonlinearity is $1.3 \%$ for a 1.5 V input range, and the cell to cell gain matching is $1 \% \mathrm{rms}$. The uniformity of the individual memory cell responses across the whole input voltage range is 10 mV rms after a simple multiplication and addition procedure. The dynamic range of the circuits is 8 bits and the power dissipation for devices, when operated from +5 V analog and +5 V digital supply levels, is 50 mW and 35 mW , respectively.

The proposed analog memories are an alternative for the camera electronics of the Cherenkov telescope where continuous data acquisition is not required.

### 8.2 Suggestions for Future Work

A number of suggestions merits to be taken in consideration for further investigation.

- A new circuit board smaller than the previous boards would be necessary to be implemented. This board must be carefully designed to minimise the perturbations caused by routed on board traces, reflections on cables, ringing of power supply, and control signals. The experimental device should be bounded directly on board and not by using a chip package and socket ( 68 pin CLCC). This configuration minimises the parasitic and cross-coupling capacitances and may increase the dynamic range and the readout speed.
- An analog calibration was used to correct data. The output voltages were measured with high impedance FET probes and their values displayed on the digital oscilloscope. Errors can occur due to the probe and oscilloscope measurements. Therefore a digital calibration would be suitable for the analog memories. The waveforms applied at the analog inputs are stored in the analog memories and then digitised by analog-to-digital converters. The digitised output voltage levels are transferred into static digital memories. These digital memories can also store the calibration constants.
- It would be possible the integration of analog-to-digital converters on a single die. This would enable an implementation of an on-chip digital correction circuit.
- The maximum sampling rate of the analog memories is limited by the delays of the inverters in the write control circuit, as explained in Section 5.2. In AMS $0.8 \mu \mathrm{~m}$ CMOS technology the sampling rate can be increased to 1 GHz by modifying the drawn dimensions of MOS transistors in the delay chains. In more advanced CMOS submicron technologies it should be possible to attain sampling speeds of 2 GHz .


## Appendix A

## Parameters

|  | Parameter | Symbol | Value | Units |
| :--- | :--- | :--- | :--- | :--- |
| NMOS Electrical <br> Parameters | electron mobility | $\mu_{n}$ | $4.63 \times 10^{-2}$ | $\mathrm{~m}^{2} / \mathrm{Vs}$ |
|  | threshold voltage | $V_{T n}$ | 0.72 | V |
|  | flicker noise coefficient | $K_{f n}$ | $2.33 \times 10^{-26}$ | - |
|  | flicker noise exponent | $A_{f n}$ | 1.451 | - |
| PMOS Electrical <br> Parameters | hole mobility | $\mu_{p}$ | $1.67 \times 10^{-2}$ | $\mathrm{~m}^{2} / \mathrm{Vs}$ |
|  | threshold voltage | $V_{T p}$ | -0.72 | V |
|  | flicker noise coefficient | $K_{f p}$ | $6.314 \times 10^{-29}$ | - |
|  | flicker noise exponent | $A_{f p}$ | 1.279 | - |
| Capacitance | oxide capacitance <br> per unit area | $C_{o x}$ | $2.16 \times 10^{-3}$ | $\mathrm{~F} / \mathrm{m}^{2}$ |

Table A.1: AMS $0.8 \mu \mathrm{~m}$ CMOS Process Parameters [40].

|  | Parameter | Symbol | Value | Units |
| :--- | :--- | :--- | :--- | :--- |
| Capacitances | write transistor gate overlap capacitance | $C_{w i}$ | 8.5 | fF |
|  | read transistor gate overlap capacitance | $C_{r i}$ | 2.5 | fF |
|  | parasitic capacitance to ground at node $x_{i}$ | $C_{p i}$ | 41 | fF |
|  | capacitance between the inverting input and <br> the output of the amplifier | $C_{p p}$ | 10.6 | fF |
|  | capacitance of the input bus to ground | $C_{i n b}$ | 4.6 | pF |
|  | capacitance of the read bus to ground | $C_{r d b}$ | 3.3 | pF |
|  | drain capacitance of the input switch | $C_{i s}$ | 116 | fF |
| Resistances | write switch on resistance | $R_{w i}$ | 180 | $\Omega$ |
|  | input switch on resistance | $R_{i s}$ | 7 | $\Omega$ |

Table A.2: Analog Memory Core Parameters.

Appendix A: Parameters

## Appendix B

## Analysis of Charge Injection in MOS Analog Switches

The error voltage induced by the turning off of a MOS switch is one of the fundamental factors that limit the accuracy of the switched capacitor circuits. A MOS transistor holds mobile charges in its channel when it is on. When the transistor turns off, some portion of the mobile charges is transferred to the storage capacitor and causes an error in the sampled voltage. The clock voltage feedthrough through the gate-drain overlap capacitance also contributes to the error. The turn off of an MOS switch consists of two distinct phases [22]-[25]. During the first phase, the transistor is on and a conduction channel extends from the source to the drain of the transistor. When the gate voltage reaches the threshold voltage, the conduction channel disappears and the transistor enters the second phase of turn off. During this phase, only the clock feedthrough through the gate-drain overlap capacitance continues to increase the error voltage.

In Figure B. 1 is shown a schematic of the NMOS switch placed in signal return path together with parasitic capacitances associated and with sampling capacitance $C_{S}$. $C_{o}$ is the gate oxide capacitance excluding overlap capacitance, $C_{p}$ is the parasitic capacitance to ground, and $C_{o v}$ is the gate overlap capacitance. The input voltage $V_{i n}$ and the dc reference voltage $V_{C}$ are supposed to be constant during this analysis.

The transistor is turned off by changing the gate voltage $V_{G}$ from the high voltage level $V_{H}$ to the low level $V_{L}$, as represented by the $P R$ segment in Figure B.1. The gate voltage is assumed to be a ramp function which begins to fall at time 0 from the high value $V_{H}$ toward the low value $V_{L}$ at a falling slope $U$,

$$
\begin{equation*}
V_{G}=V_{H}-U t . \tag{B.1}
\end{equation*}
$$

As long as the transistor is in the ohmic region $\left(V_{H} \geq V_{G} \geq V_{C}+V_{T}\right)$, which corresponds to the $P Q$ segment in Figure B.1, the drain-to-source current can be described as

$$
\begin{equation*}
I_{D S}=\beta\left(V_{G S}-V_{T}-\frac{V_{D S}}{2}\right) V_{D S} \tag{B.2}
\end{equation*}
$$

where $V_{D S}=V_{D}-V_{C}$ is the transistor drain-to-source voltage, $V_{G S}=V_{G}-V_{C}$ is the transistor gate-to-source voltage, $V_{T}$ is the threshold voltage, $\beta=\mu_{n} C_{o x} W / L, \mu_{n}$ is the


Figure B.1: Schematic of the NMOS switch placed in signal return path.
electron mobility in the channel, $C_{o x}$ is the oxide capacitance per unit area, and $W$ and $L$ are the channel width and length of the transistor, respectively. For small drain-to-source voltages (B.2) can be approximated by

$$
\begin{equation*}
I_{D S}=\beta\left(V_{G S}-V_{T}\right) V_{D S} \tag{B.3}
\end{equation*}
$$

If (B.1) is inserted into (B.3),

$$
\begin{equation*}
I_{D S}=\beta\left(V_{H T}-U t\right) V_{D S} \tag{B.4}
\end{equation*}
$$

where $V_{H T}=V_{H}-V_{C}-V_{T}$.
From the Kirchhoff's Current Law applied at node $A$ in Figure B.1,

$$
\begin{equation*}
C_{e q} \frac{d V_{D S}}{d t}=-\beta\left(V_{H T}-U t\right) V_{D S}-\left(C_{o v}+\frac{C_{o}}{2}\right) U \tag{B.5}
\end{equation*}
$$

where

$$
\begin{equation*}
C_{e q}=C_{p}+C_{o v}+\frac{C_{o}}{2}+C_{S} \tag{B.6}
\end{equation*}
$$

The solution of the differential equation [37,38] with the boundary condition $V_{D S}(0)=0$ is

$$
\begin{align*}
& V_{D S}(t)=-\frac{C_{o v}+\frac{C_{o}}{2}}{C_{e q}} \sqrt{\frac{\pi U C_{e q}}{2 \beta}} \exp \left[\frac{\beta U}{2 C_{e q}}\left(t-\frac{V_{H T}}{U}\right)^{2}\right] \times \\
& \times\left\{\operatorname{erf}\left(\sqrt{\frac{\beta}{2 U C_{e q}}} V_{H T}\right)-\operatorname{erf}\left[\sqrt{\frac{\beta}{2 U C_{e q}}}\left(V_{H T}-U t\right)\right]\right\} . \tag{B.7}
\end{align*}
$$



Figure B.2: Analysis of clock feedthrough effect for NMOS switch placed in signal return path when (a) $V_{G}=V_{C}+V_{T}$ and (b) $V_{G}=V_{L}$.

At $t_{Q}=V_{H T} / U$ which corresponds to the $Q$ point in Figure B.1, the threshold condition is reached ( $V_{G}=V_{C}+V_{T}$ ) and the first phase ends. The error voltage at this time is

$$
\begin{equation*}
V_{D S}\left(t_{Q}\right)=-\frac{C_{o v}+\frac{C_{o}}{2}}{C_{e q}} \sqrt{\frac{\pi U C_{e q}}{2 \beta}} \operatorname{erf}\left(\sqrt{\frac{\beta}{2 U C_{e q}}} V_{H T}\right) \tag{B.8}
\end{equation*}
$$

It is well known that

$$
\operatorname{erf}(x) \approx \begin{cases}1 & \text { if } x \gg 1  \tag{B.9}\\ \frac{2 x}{\sqrt{\pi}} & \text { if } x \ll 1\end{cases}
$$

therefore, (B.8) can be simplified for fast switching-off

$$
\begin{array}{r}
\frac{\beta V_{H T}^{2}}{2 C_{e q}}
\end{array}<U
$$

where $V_{p 1}$ is the pedestal voltage due to the charge injection. Assuming that $\alpha$ is a coefficient $(0<\alpha<1), C_{o}=C_{o x} W L$ where $C_{o x}$ is the oxide capacitance per unit area, then (B.10) can be written as follows

$$
\begin{equation*}
V_{p 1}=-\frac{\alpha C_{o x} W L}{2 C_{S}}\left(V_{H}-V_{C}-V_{T}\right) \tag{B.11}
\end{equation*}
$$

After the transistor turns off $\left(V_{G} \leq V_{C}+V_{T}\right)$, only the gate overlap capacitance contributes to the pedestal voltage. In order to calculate the pedestal voltage due to
the clock feedthrough effect, two configurations were proposed in Figure B.2. The total charge at node $A$ in Figure B.2(a) is

$$
\begin{equation*}
Q_{A}^{(a)}=C_{p}\left(V_{D S 1}+V_{C}\right)+C_{S}\left(V_{D S 1}+V_{C}-V_{i n}\right)+C_{o v}\left(V_{D S 1}-V_{T}\right) \tag{B.12}
\end{equation*}
$$

and in Figure B.2(b) is

$$
\begin{equation*}
Q_{A}^{(b)}=C_{p}\left(V_{D S 2}+V_{C}\right)+C_{S}\left(V_{D S 2}+V_{C}-V_{i n}\right)+C_{o v}\left(V_{D S 2}+V_{C}-V_{L}\right) \tag{B.13}
\end{equation*}
$$

The charge conservation $\left(Q_{A}^{(a)}=Q_{A}^{(b)}\right)$ and the voltage difference $\left(V_{D S 2}-V_{D S 1}\right)$ defined as the pedestal voltage due to the clock feedthrough effect $V_{p 2}$ yield

$$
\begin{equation*}
V_{p 2}=-\frac{C_{o v}}{C_{o v}+C_{S}+C_{p}}\left(V_{C}-V_{L}+V_{T}\right) . \tag{B.14}
\end{equation*}
$$

The total pedestal voltage $V_{p}$ after turn off of the sampling switch is then

$$
\begin{equation*}
V_{p}=V_{p 1}+V_{p 2} . \tag{B.15}
\end{equation*}
$$

## Appendix C

## FASTSAMP-EV Chip Test Setup

The test setup used to evaluate the performance of the FASTSAMP-EV chip is described in detail in this appendix. Figure C. 1 illustrates the configuration of the instruments for the performance tests, while the instruments are identified in Table C.1. The chip was mounted on a printed circuit board (PCB) together with the supporting circuitry such as commercial amplifiers, resistors and capacitors. Only low speed digital input and output ports are required to control the circuit and to read out the measured data. The board can thus be operated without an elaborate high speed data acquisition system.

The test board was mounted in an aluminium box and the digital control signals were transmitted on LEMO cables to minimise the noise pick-up. The acquisition of the measured data was controlled by a Hewlett Packard workstation via GPIB [52] interface connected to the digitising oscilloscope TDS 420A [53, 55], as indicated in Figure C.1. A digital test equipment HP 82000 [56] was used to generate external signals necessary for the chip. The analog input waveforms were generated by a waveform generator AWG 2041 [57] and the supply voltages, +5 V analog and digital, were provided by a triple linear dc power supply IC-TRIPLE-100. The software used for control and data processing was written in C and C++ programming languages [35, 36]. The graphical HP VEE [58] data acquisition software was used to control the instruments and process the data.

The schematic for the PCB was entered on a workstation using CONCEPT [49, 50] schematic design software, and the board was laid out using the ALLEGRO [51] layout editor. A gerber file was then created, and the board was fabricated at ASIC laboratory in Heidelberg. The board measures $12 \mathrm{~cm} \times 24 \mathrm{~cm}$ and consists of two layers.

Shown in Figure C. 2 is the schematic of the board including the chip and the power supply connections. The chip was mounted on board in a socket ( 68 pin CLCC). The power for the analog and digital components is separated on PCB, as is the ground, to minimise feedthrough from the digital signals to the analog circuits. Outside the PCB, the analog ground and digital ground are connected together to ensure the functionality of the circuit. The power supplies $P_{1}-P_{3}$ together with filter capacitances $C_{11}-C_{16}$ provide +5 V analog, +5 V digital, and +2.5 V reference voltage. Each chip power supply pin has its own ceramic decoupling capacitor as identified by $C_{1}-C_{10}$.

In Figure C. 3 are shown the connections between the chip and other components such as commercial amplifiers, resistors and capacitors. All input digital signals around


Figure C.1: Experimental setup for FASTSAMP-EV chip.
(A) Tektronix TDS 420A Digitising Oscilloscope
(B) Sony/Tektronix AWG 2041 Arbitrary Waveform Generator
(C) IC-TRIPLE-100 Linear Triple Power Supply
(D) Hewlett Packard HP 82000 Test Equipment

Table C.1: Test setup equipment list for FASTSAMP-EV chip.
the chip are connected by LEMO coaxial cables to the HP 82000 test equipment. The LEMO cables are transmission lines and have a characteristic impedance of $50 \Omega$. To avoid reflections on cables, every transmission line is terminated in a $50 \Omega$ resistor on PCB, as represented by the resistors $R_{1}-R_{27}$ and $R_{36}-R_{39}$, respectively. The analog signals applied at the inputs of the test board are ac coupled to the chip by the capacitors $C_{17}-C_{20}$ of $1 \mu \mathrm{~F}$ value and the dc voltages generated by the power supplies $P_{4}-P_{7}$ are superimposed via $10 \mathrm{k} \Omega$ resistors $R_{40}-R_{43}$. Since these dc voltages can be changed, they can be used to generate the dc calibration voltage levels during the calibration phase. The outputs are buffered by the AD645 [59] operational amplifiers $U_{33}-U_{36}$. The AD645 is a low noise, high input impedance (FET) commercial amplifier, an excellent choice for high impedance applications where stability is of prime concern. $C_{21}-C_{28}$ serve for decoupling and are ceramic capacitors. In order to ensure a speed in the four servo feedback circuits of the chip, four resistors $R_{28}-R_{31}$ are connected to power supply and other four resistors $R_{32}-R_{35}$ to ground, respectively.

The operation of the circuit can be described into write and read phases. For testing the chip , 50 write cycles and one read cycle were sufficient. One sequence of 65000 vectors including 50 write cycles and one read cycle was repeated at infinite and each vector of the sequence was set to 32 ns. Figure C. 4 and Figure C. 5 show the vector diagrams for write and read phases.

$$
\begin{gathered}
\text { vdda }=+5 \mathrm{~V}-\text { Analog Power Supply } \\
\text { gnda }- \text { Analog Ground } \\
\text { vdd }=+5 \mathrm{~V}-\text { Digital Power Supply } \\
\text { gndd }- \text { Digital Ground } \\
\text { RefVoltage }=\mathrm{V}_{\mathrm{B}}=\mathrm{V}_{\mathrm{C}}=+2.5 \mathrm{~V} \text { - Reference Voltage } \\
\mathrm{V}_{\mathrm{B}}, \mathrm{~V}_{\mathrm{C}}-\text { Reference Voltages for Analog Memory Core }
\end{gathered}
$$



Figure C.2: Schematic of the Printed Circuit Board of FASTSAMP-EV chip. Power supply connections.


Figure C.3: Schematic of the Printed Circuit Board of FASTSAMP-EV chip. Connections between the chip and other components.

$$
\begin{aligned}
& \text { In1 } \\
& \text { Aref1 }
\end{aligned}
$$



## Appendix D

## FASTSAMP-V1 Chip Test Setup

This appendix describes the test setup for FASTSAMP-V1 chip. The configuration of the instruments is shown in Figure D. 1 and the instruments are identified in Table D.1. The steps for the acquisition data are explained in detail in Appendix C. To reduce the ground noise in this configuration the digital test equipment HP 82000 has been replaced by the data generator DG 2020A [60].

The printed circuit board (PCB) measures $14 \mathrm{~cm} \times 14 \mathrm{~cm}$ and was mounted in an aluminium box. The board has two layers and was fabricated at ASIC laboratory in Heidelberg. The test board was laid out using the same software as for the PCB of FASTSAMP-EV chip.

The schematic of the board including the chip and the power supply connections is shown in Figure D.2. The connections of the power supply are similar as for the previous chip FASTSAMP-EV.

Figure D. 3 shows the connections of the chip with a Generic Array Logic (GAL), counters, commercial amplifiers, resistors and capacitors. The digital input signals are connected to the DG 2020A data generator by LEMO coaxial cables and are terminated on PCB by $50 \Omega$ resistors. The configurations for the analog inputs as well as for the analog outputs are the same as in the test board of FASTSAMP-EV chip. A clock signal Clock of 15.625 MHz is connected to the counters $U_{2}-U_{3}$ and to the GAL.

Two 4-bit binary counters 74AS163 [61] were used to provide the address signals $a 0$ through $a 7$ necessary for the GAL device. The counters are on 8-bit cascading configuration and each of them has an internal look ahead circuitry for fast counting. The clear function for both counters is synchronous. Setting up a high level at the load enables the counters to be in the counting mode for all time. All unused inputs are connected to the ground to improve noise immunity and reduce the current for the devices. Each power supply pin of the counters is decoupled to ground by ceramic capacitors $C_{17}$ and $C_{18}$.

A programmable device GAL is employed to produce the control signals necessary for the chip. The GAL26CV12 [62], at 4.5 ns maximum delay time from clock input to data output, combines a high performance CMOS process with Electrically Erasable ( $\mathrm{E}^{2}$ ) floating gate technology. This technology offers high speed erase times, providing the ability to re-program or reconfigure the device quickly and efficiently. The code for the GAL was written using ABEL-HDL [63] design software and the device was programmed


Figure D.1: Experimental setup for FASTSAMP-V1 chip.
(A) Tektronix TDS 784A [54, 55] Digitising Oscilloscope
(B) Sony/Tektronix AWG 2041 Arbitrary Waveform Generator
(C) IC-TRIPLE-100 Linear Triple Power Supply
(D) Sony/Tektronix DG 2020A Data Generator

Table D.1: Test setup equipment list for FASTSAMP-V1 chip.
in registered mode by ISP SYNARIO [64] programming system. Unused inputs are connected to ground to reduce the power consumption on device and to reduce the noise. A ceramic capacitor $C_{19}$ serves for decoupling the power supply of the device.

To test the chip, one sequence of 65000 vectors which covers the write and read phases was repeated at infinite. One sequence consists of 50 write cycles and one read cycle. In figure D. 4 is shown the vector diagram for the write phase including also the signals which are provided by GAL. One read cycle is represented in Figure D.5. For both phases each vector of the sequence was set to 32 ns .


Figure D.2: Schematic of the Printed Circuit Board of FASTSAMP-V1 chip. Power supply connections.


Figure D.3: Schematic of the Printed Circuit Board of FASTSAMP-V1 chip. Connections between the chip and other components.

Figure D.4: Vector diagram for write phase of FASTSAMP-V1 chip.


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